

# The Polyphase Duplex Slide Rule

A Self Teaching Manual tables of settings, equivalents and gauge points

By William E. Breckenridge, A. M. Associate in Mathematics Columbia University New York City



Published by

# **KEUFFEL & ESSER CO.**

NEW YORK, 127 Fulton Street,

General Office and Factories, HOBOKEN, N. J.

516-20 S. Dearborn St. 817 Locust St.

SAN FRANCISCO 30-34 Second St.

MONTREAL 7-9 Notre Dame St., W.

Drawing Materials, Mathematical and Surveying Instruments, Measuring Tapes.



# K & E POLYPHASE DUPLEX SLIDE RULE.



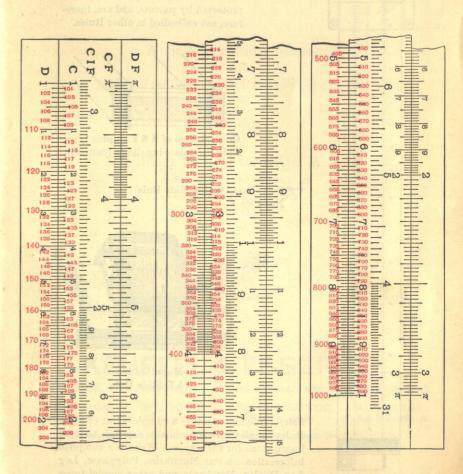
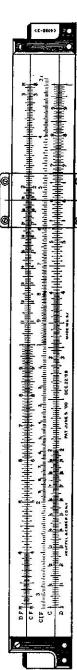


Diagram illustrating the reading of the graduations of the rule.

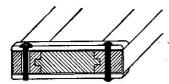


No. 4088-8. Front

The Slide Rule in its present form has become an indispensable aid not only to the engineer and scientist, but also to the manufacturer, the merchant, accountant, and all others whose occupation or business involves calculations.

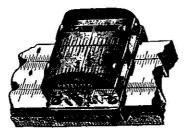
We manufacture slide rules and devote to them a separate department of our factory which is thoroughly equipped with the most improved special machinery.

Several of our improvements are protected by patents, and are, therefore, not embodied in other Rules.



Cross section of K & E Duplex type Slide Rule showing slide adjustment

Polyphase Duplex Slide Rule
No. 4088-3.



Magnifier for K& E Slide Rule.

Note:- We manufacture a complete line of Slide Rules for all uses and publish a separate book of instructions for each type. Write for complete information on our Mannheim, Polyphase, Log Duplex, Merchants, and other special types of Slide Rules.

# The Polyphase Duplex REG. U. S. PAT. OFF. Slide Rule

A Self Teaching Manual with tables of settings, equivalents and gauge points

By
William E. Breckenridge, A. M.
Associate in Mathematics
Columbia University
New York City



Published by

# **KEUFFEL & ESSER CO.**

NEW YORK, 127 Fulton Street,

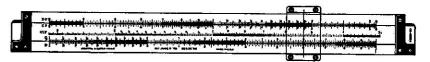
General Office and Factories, HOBOKEN, N. J.

CHICAGO S 516-20 S. Dearborn St. 8

ST. LOUIS 817 Locust St. SAN FRANCISCO 80-84 Second St. MONTREAL 7-9 Notre Dame St., W.

Drawing Materials, Mathematical and Surveying Instruments, Measuring Tapes.

Copyright 1924, by KEUFFEL & ESSER CO.



# THE POLYPHASE DUPLEX SLIDE RULE.

# PREFACE.

This manual is designed to meet the needs of all who desire to learn the use of this slide rule.

Chapter 1, through the use of numerous cuts and examples simply explained, is self-teaching. Some persons will learn all that they require from a few lessons in this chapter.

It is suggested that everyone learning to use the slide rule begin by working the problems in Chapter I.

In Chapters II, III, IV, and V, a simple explanation of the theory of the slide rule is followed by the advanced subjects of Cubes, Cube Root, Sines, Cosines, Tangents, Logarithms, and the Solution of Triangles.

Special work for technical men and typical problems from various occupations are presented in Chapters VI, VII, and VIII.

# WHO SHOULD USE THE SLIDE RULE?

- I. Teachers in the following types of schools:
  - 1. Elementary Schools in the higher grades.
  - 2. Junior High Schools for part of their practical mathematics.
  - High Schools in connection with logarithms, practical mathematics, or trigonometry.
  - Colleges in their courses in algebra or trigonometry. Most colleges
    have already made the slide rule a part of the trigonometry course.
  - Evening schools; since no subject holds the students so well as the teaching of the use of the slide rule.
  - 6. Engineering and Trade Schools find the rule indispensable.
- Engineers, Mechanics, Chemists, and Architects who have long understood its value.
- III. Private Secretaries to check reports by the slide rule in a small fraction of the time required by ordinary calculation.
- IV. Estimators, Accountants and Surveyors to make approximate calculations rapidly and with sufficient accuracy to check gross errors.

By means of the slide rule, all manner of problems involving multiplication, division and proportion can be correctly solved without mental strain and in a small fraction of the time required to work them out by the usual "figuring."

For instance, rapid calculation is made possible in the following everyday problems of office and shop: estimating; discounts; simple and compound interest; the conversion of feet into meters, pounds into kilograms and foreign money into U. S. money; the taking of a series of discounts from list prices; and adding profits to costs. Dozens of equivalents are instantly found, such as cubic inches or feet in gallons, and vice versa; centimeters in inches; inches in yards or feet; kilometers in miles; square centimeters in square inches; liters in cubic feet; kilograms in pounds; pounds in gallons; feet per second in miles per hour; circumferences and diameters of circles.

# How much education is necessary?

Anyone who has a knowledge of decimal fractions can learn to use the slide rule.

# How much time will it take?

The simplest operations may be learned in a few minutes, but it is recommended that at least the problems in Chapter I be worked thoroughly and checked by the answers, in order to gain accuracy and speed. This will take from one to ten hours, according to the previous training of the student.

# How accurate is the Slide Rule?

The accuracy of the slide rule is about proportional to the unit length of the scales used.

The 10 inch scale gives results correct to within about 1 part in 1000, or one tenth of one per cent.

The 20 inch scale gives results correct to within one part in about 2000.

The Thacher Cylindrical slide rule gives an accuracy of about 1 part in 10000.

# How to use this manual

For the man who desires to perform the simplest operations of multiplication and division, the first few lessons in Chapter I will be sufficient. Work the illustrative examples and as many problems for practice as seem necessary to obtain accuracy and speed.

For educational use, Chapter II furnishes the necessary theory and history of the rule, while Chapter I provides additional examples for practice. Chapters III, IV, and V may be used for advanced work.

# CHAPTER I

# ESSENTIALS OF THE SLIDE RULE SIMPLY EXPLAINED

The slide rule is an instrument that may be used for saving time and labor in most of the calculations that occur in the practical problems of the business man, mechanic, draftsman, engineer, or estimator.

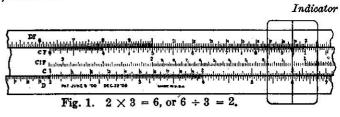
On scales C and D (front face), if 1 at the extreme left is taken as unity, then 1 at the extreme right of these scales is 10.

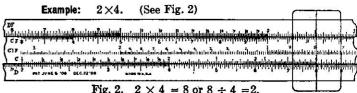
On scales A and B (rear face), if 1 at the extreme left is taken as unity then 1 in the middle of the scale is 10 and 1 at the extreme right is 100.

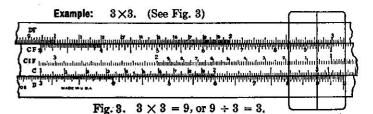
In order that you may see how the rule is used on simple problems where you know the answers, let us take the following:

Example:  $2 \times 3$ . (See Fig. 1)

Opposite 2 on scale D set 1 on scale C. Then move the indicator or glass runner so that the hair line is over 3 on scale C. Directly below this 3 you will find 6, the answer.







Example:  $6 \div 3$ . (See Fig. 1)

Opposite 6 on scale D, set 3 on scale C. Look along C to the left, till you come to 1 at the end of the slide. Under this 1 you will find 2, the answer, on scale D.

Example: In the same way find  $8 \div 4$ . (See Fig. 2) Example: " "  $9 \div 3$ . (See Fig. 3)

It will be noted that the cuts shown are not in the same scale. This arrangement is for the purpose of illustrating various lengths of the rule.

# SQUARES AND SQUARE ROOTS

**Example:** You will remember that to square a number means to multiply that number by itself;  $e. g., 3^2$  means  $3 \times 3 = 9$ . On the slide rule this is done as follows: set the hairline of the glass indicator to 3 on scale D. Above, on scale A, under the hairline, you will find 9, the answer. (Fig. 4).

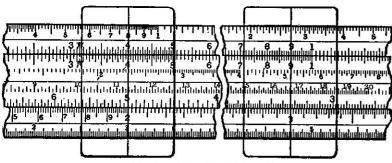


Fig. 4.  $3^2 = 9$  and  $2^3 = 4$ .

Example: In the same way find 22. (See Fig. 4)

To find square roots simply do the work in the reverse order.

To find the square root of 9, find the number which multiplied by itself will give 9. The square root of 9 is indicated thus:  $\sqrt{9}$ .

Set the indicator to 9 on scale A, being careful to use the 9 on the left-hand half of the rule, because the other 9 is really 90. Below, on scale D, find 3, the answer. (Fig. 4).

Example: Find  $\sqrt{4}$ .

Set the indicator to 4 on A. Under the indicator on scale D, find 2, the answer. (Fig. 4).

We shall now proceed to apply the same methods to numbers of two or more figures.

# MULTIPLICATION OF TWO OR MORE FIGURES

Example: Find the value of  $2 \times 1.5$ .

Opposite 2 on D (front face) set 1 on C. Move the indicator to 1.5 on C. This will be between 1 and 2 at the division numbered 5; since the numbered divisions between 1 and 2 on C and D are the tenths. Under the indicator, find 3 on D. (Fig. 5)

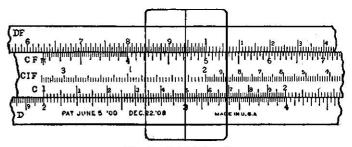
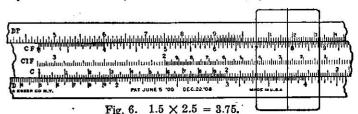


Fig. 5.  $2 \times 1.5 = 3$ .

Example:  $2 \times 1.8$ . Using Fig. 5, see if you can make it 3.6.

**Example:**  $1.5 \times 2.5$ . Opposite 1.5 on D set 1 on C. Move the indicator to 2.5 on C. Below 2.5, find 3.75, the answer, on D. Note that this answer is halfway between 3.7 and 3.8, which makes it 3.75. (Fig. 6).



HOW TO READ THE SCALES

Graduations on the slide rule are not measures of length, but represent figures.

On the 8" and 10" slide rules, scales C and D consist of nine prime spaces of unequal length; the first line of each space is numbered, respectively, 1 (called left index), 2, 3, 4, 5, 6, 7, 8, 9,; the last line is numbered 1, and is called the right index. The spaces 1-2, 2-3, 3-4, etc., decrease in length, the space from 1 to 2 being the longest and every succeeding space being shorter than the one preceding it.

Each of these prime spaces is divided into ten (secondary) spaces, also decreasing in length, the nine lines between prime 1 and prime 2 being numbered 1, 2, 3, 4, 5, 6, 7, 8, 9, in smaller figures than those of the prime graduations. Space does not permit the numbering of the other secondary lines.

Each of the spaces between these secondary lines is again subdivided. Thus, each secondary space between prime 1 and prime 2 is divided into ten (unequal) parts, The secondary spaces between prime 2 and prime 4 are subdivided into five (unequal) spaces.

The secondary spaces from 4 to the end are subdivided into two (unequal) parts by one line between the two secondary lines.

To find a number, always read the first figure to the left on the prime line, the second figure of the number on the secondary line to the right thereof, and the third figure on the subdivision; thus, to read 435 (say four, three, five, not four hundred and thirty-five) find prime 4, secondary 3 and sub. 5.

## PLACING THE DECIMAL POINT

Example:  $2 \times 15$ .

This is worked on the rule exactly like the above examples, but you can see by looking at the problem that the answer is 30 and not 3.

# **Problems**

- 1.  $20 \times 15$ . 2.  $200 \times 15$ .
- 3.  $20 \times 150$ .
- 4.  $2 \times .15$ .
- 5.  $2 \times .015$ . 6.  $.2 \times 15$ .
- 7.  $.02 \times .015$ .

All of these problems are worked like the above. As far as the slide rule is concerned, we multiply 2 by 1.5 and get 3. Then we place the decimal point by inspection. From arithmetic we remember that in multiplying decimals we first multiply as though there were no decimal points, then point off as many decimal places in the answer as there are total decimal places in the two numbers which were multiplied together. Thus, in Problem 7, there are two decimal places in .02 and three in .015. So in the answer, 30, we must have 2+3, or 5 places, making the result .00030. Of course the 0 at the right does not count and the final result is .0003.

From the above explanation it is evident that the decimal point is not considered in operating the slide rule. After the work of the rule has been done, the decimal point can usually be placed by inspection; i. e. through a mental survey of the influence of the involved factors upon the result. Where this is not feasible, a rough arithmetical calculation will serve to properly locate the decimal point.

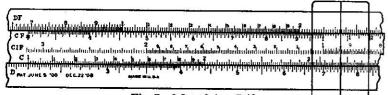


Fig. 7.  $2.2 \times 3.4 = 7.48$ .

Example:  $2.2 \times 3.4$ .

Opposite 2.2 on D set 1 on C. Move the indicator to 3.4 on C. Under the hair line on D find 748.

That the unit figure is 8 is further confirmed by observing that the product of the unit figures 2 and 4 in the example is 8.

Since  $2.2 \times 3.4$  is roughly  $2 \times 3$ , or 6, place the decimal point in 748 so that the result will be as near 6 as possible. Evidently the answer is 7.48. (Fig. 7).

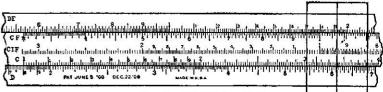


Fig. 8.  $18 \times 3.4 = 61.2$ 

Example:  $18 \times 3.4$ .

Using the same method as in the previous example, the slide rule gives 612. By a rough calculation the problem is about equal to  $20 \times 3 = 60$ . Hence we make 612 look like 60 by placing the decimal point after the 1. The answer is 61.2.

Example:  $16 \times 2.4$ . Answer 38.4. Example:  $1.4 \times 2.6$ . Answer 3.64.

Problem 8. Fill in the blanks in the following multiplication table, using the slide rule:

	21	22	23	24	25	26	27	28	29
31									
32									
33	N								
34									

Set left index of C to 31 on D. Note that the factors 21 to 29 can be taken without resetting the slide.

## WHICH INDEX TO USE

If we attempt to multiply 30 by 45, using the preceding methods of setting the 1 on the left hand end of C to 30 on D, we shall find it impossible to move the indicator to 45, since 45 on scale C lies beyond the right hand end of scale D. In such a case, begin the work on the rule by setting the 1 on the right hand end of C to 30 on scale D. It is then possible to set the indicator to 45 on C. Opposite the 45 on C find 135 on D. Placing the decimal point by inspection, the result is 1350. Or we may read the answer 1350 on DF oppostie 45 on CF, the folded rule doing away with the necessity of shisting the slide.

We will now define the left hand 1 on scale C as the left index and the right hand 1 on scale C as the right index. In most examples, the following rule will be found useful in determining which index to use:

If the product of the first figures of the given numbers is less than 10, use the left index: if this product is greater than 10, use the right index.

Example 1.  $2.13 \times 3.33$ ,  $3 \times 2 = 6$ . Use the left index.

Example 2.  $7.23 \times 4.71$ ,  $7 \times 4 = 28$ . Use the right index. Example 3.  $.131 \times 4.6$ .  $1 \times 4 = 4$ . Use the left index.

An exception to this rule will be found in such a case as  $3.12 \times 3.31$ . According to the rule the left index should be used. It will be found, however, that it is necessary to use the right index. This is due to the fact that while the product of the first figures of the two numbers is less than 10, the product of the complete numbers is greater than 10.

In most cases, the use of the above rule will save time.

## PER CENT

Example: Suppose you are earning 56 cents per hour and you are given an increase of 8 cents. What per cent increase do you receive?

Of course you will divide 8 by 56.

To divide one number by another on the slide rule we simply reverse the order of the work we have been doing in multiplication.

Set the indicator to 8 on scale D.

Move the slide so as to set 56 on C to the hair line of the indicator.

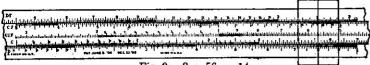


Fig. 9.  $8 \div 56 = .14$ .

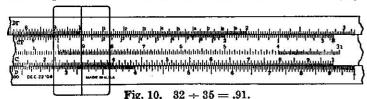
Under 1 on C we find 14 and a little over. But the result is nearer 14 than 15. Hence the correct result to two figures is 14. By inspection the decimal point must be placed before the number, making the answer .14 or 14 per cent.

Example: A man earned 35 cents per hour. He learned a new trade which increased his earning power to 67 cents per hour. What per cent increase did he receive?

His increase is 32 cents per hour. The per cent of increase is found by dividing 32 by 35.

Set the indicator to 32 on D.

Set 35 on C to the indicator. The result cannot be found under the left index i.e. the 1 at the extreme left of scale C, since this projects beyond scale D. So we use the right index of C. Under this index, find 91 on scale D. (Fig. 10).



In the same way, for practice, try the following, obtaining the result correct to two figures:

Problem 9. What per cent of 91 is 45?

(Divide 45 by 91)

- 10. What per cent of 73 is 24?
- 11. What per cent of 67 is 61?
- 12. What per cent of 53 is 31?
- 13. What per cent of 82 is 13?
- 14. What per cent of 42 is 9?

If you have a long report to make out in which a large number of per cents are to be calculated, why not use the slide rule?

A secretary to the president of a big corporation recently said: slide rule does my work in one-third of the time that would be required otherwise."

# READING TO THREE FIGURES

Suppose you had to get per cents in a problem like the following:

Example: A baseball player made 57 hits out of 286 times at bat. What is his percentage?

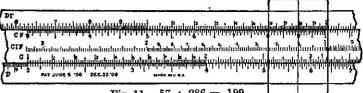


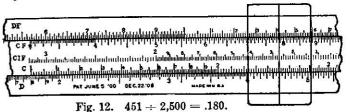
Fig. 11.  $57 \div 286 = .199$ .

Opposite 57 on D set 286 on C. When we look for 286 we observe that between 2.8 and 2.9 there are five spaces on the rule. Hence every space counts one-fifth of .1, which is .02. Since we want six points for the third figure, we have to use three spaces, every one worth .02.  $3 \times .02 = .06$ .

Under the left index of Clook for the result on D. When we read this result, we see that it comes on the rule between 1.9 and 2.0. There are ten small spaces between 1.9 and 2.0. Hence every space counts one point. The index is close to the ninth of these divisions. Hence the reading is 199. Now we must place the decimal point. A rough calculation shows that  $\frac{57}{286}$  is nearly  $\frac{60}{300}$ , or  $\frac{1}{5}$ . Hence the decimal point must be placed so as to make the result some-

where near one-fifth or .2. Evidently the result is .199. This may be read 199/10 per cent or 199/10 hundredths, or 199 thousandths.

Example: If your income is \$2,500 per year and you save \$451, what per cent do you save?



Opposite 451 on D set 25 on C. Under the index find 180 on D. Hence the answer is .180, or 18 per cent. We note that when we look for the 1 in 451 on the rule, we find only two spaces between 45 and 46. Hence each space counts one-half of a hundredth or one-half of .01, which is .005 or five points for the third figure. We estimate one-fifth of the small space to obtain .001. (Fig. 12)-

Example: If your salary is \$57.50 per week, and you are given an increase of \$12.40, what per cent increase do you receive?

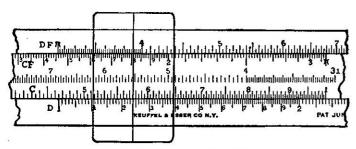


Fig. 13,  $12.4 \div 57.5 = .216$ .

Opposite 124 on D set 575 on C. This means that between 5 and 6 on C we must take 7 of the large divisions and one of the small divisions. Under the right-hand index read 216 on D. Hence the answer is  $21\frac{6}{10}$  per cent.

Problem 15.  $5.42 \div 2.42$ .

16.  $7.35 \div 3.14$ .

17.  $6.13 \div 4.61$ .

18.  $9.56 \div 7.26$ .

24.  $.0385 \div .0014$ 

19. 10 + 3.14. For 10, use either the right or left index.

 $.038 \div .001 = 38$ .

In the following problems the location of the decimal point is determined by working the problems in round numbers.

Problem 20.  $16.5 \div .245$  is approximately  $16 \div .2 = 80$ . 21.  $.00655 \div .00034$  " "  $.0060 \div .0003 = 20$ . 22.  $.00156 \div 32.8$  " "  $.0015 \div 30 = .00005$ . 23.  $.375 \div .065$  " "  $.36 \div .06 = 6$ .

There is another method of placing the decimal point in division. Work the problem as though both dividend and divisor were integers (i. e., not decimals), pointing off as usual. Move the decimal point to the left as many places as there are decimal places in the dividend. Then move it to the right as many places as there are decimal places in the divisor. For example in problem 20,  $165 \div 245$  gives .673. Move the point one place to the left because there is one decimal place in the dividend, giving .0673. Then move it three places to the right because there are three places in the divisor, giving as a result 67.3. Try both methods and see which one you like the better. Let one check the other.

# MORE THAN THREE FIGURES IN A FACTOR

Suppose we have more than three figures, as in the following example: **Problem 25.** Find the circumference of a wheel 28 inches in diameter.

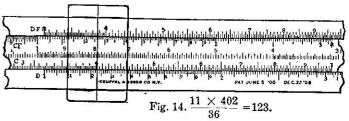
Here we must multiply 28 by 3.1416. But the  $10^{\circ}$  slide rule only reads to three figures. So cut off the fourth and fifth figures in 3.1416 and call it 3.14, since the number is nearer 3.14 than 3.15. It is, however, somewhat more convenient to work this problem on the DF scale, where  $\pi$  (3.1416) is accurately marked. Opposite 28 on D find 879 on DF.

Problem 26. Multiply 26 by 8.149. Call 8.149 equal to 8.15,

# COMBINED MULTIPLICATION AND DIVISION

**Example:** If bell metal is made 25 parts of copper to 11 parts of tin, find the weight of tin in a bell weighing 402 pounds.

The tin is evidently eleven thirty-sixths of 402, or  $\frac{11 \times 402}{36}$ .



Opposite 11 on D set 36 on C. (Fig. 14) Move the indicator to 402 on C.

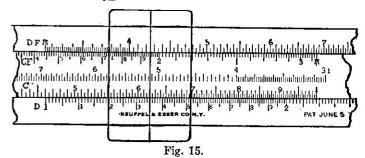
Opposite 402 on C read 123 on D.

To place the decimal point, make a rough calculation as follows: The example is roughly equal to  $\frac{10 \times 400}{40} = 100$ . So make 123 look as nearly like 100 as possible by placing the point after 3. The answer is 123 pounds of tin.

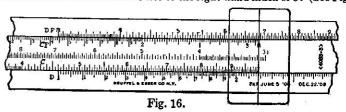
Problem 27. 
$$\frac{14 \times 525}{47}$$

Problem 28.  $\frac{24.5 \times 43.4}{3620}$ 

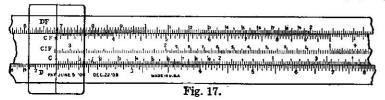
Example:  $\frac{1.35 \times 3.16}{6.2}$  (See Fig. 15)



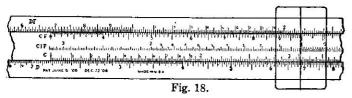
Opposite 1.35 on D, set 6.2 on C. If we try to move the indicator to 316 on C, it is impossible because 316 lies beyond the extremity of D. In such a case proceed as follows: Move the indicator to the right-hand index of C. (See Fig. 16)



Then move the slide, setting the left-hand index of C to the indicator. (Fig. 17.)



Now we can move the indicator to 316 on C. (Fig. 18.)



and under 316 on C read the answer 688 on D.

A rough calculation for the decimal point gives us  $\frac{1 \times 3}{6} = \frac{3}{6}$ , or .5. Making 688 look as much as possible like .5, we have .688.

#### **Another Method:**

Opposite 135 on *DF*, set 62 on *CF*. Move the indicator to 316 on *C*. Opposite 316 on *C* read 688 on *D*.



Example:

$$\frac{228 \times .0125}{4.36}$$

To 2.28 on D, set 4.36 on C.

Move the indicator to 1.25 on CF.

On DF, opposite the indicator, read 654.

NOTE.—In problems like the two preceding examples the method given with the first may always be avoided provided the setting on the folded scales is so chosen as to keep at least half of the slide within the groove. For this purpose there is always a choice between starting on DF, as in the first example or or on D, as in the second example.

The rough calculation for the decimal point might be  $\frac{2 \times .012}{4} = .006$ .

The answer is .00654.

Problem 29. 
$$\frac{7.63 \times 2.34}{24.3}$$

Work problems 30, 31, 32, using scales CF and DF.

Problem 30. 
$$\frac{2.56 \times 1.78}{7.4}$$

Problem 31. 
$$\frac{82.5 \times 9.3}{56.5}$$

Problem 32. 
$$\frac{32.6 \times 22.1}{9.25}$$

# PROPORTION

**Example:** If an aeroplane flying 100 miles an hour travels 86 miles in a given time, how far will an automobile traveling 22 miles an hour go in the same time? Writing this in the form of a proportion:

$$100: 22 = 86: x$$

which means that 100 is to 22 as 86 is to the answer.

The work on the rule is as follows:

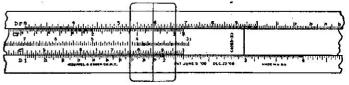


Fig. 19. 100:22=86:18.9.

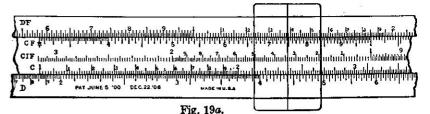
Opposite 22 on D, set 100 on C. (Use right index for 100). Opposite 86 on C read the answer, 18.9 on D. An easy method of remembering this is:

In placing the decimal point, note that 100 has the same relation to 22 that 86 has to the answer. Since 22 is about one-fifth of 100, we must place the decimal point in 189 so that the answer shall be about one-fifth of 86. Hence the answer is 18.9.

In the same way solve the following proportions:

Example: 2.54:4.72 = 7:48:xTo 472 on D, set 254 on C.

Above 748 on CF, find 139 on DF.



The result is 13.9

**Problem 36.** If a post 13.2 feet high casts a shadow 27.2 feet long, how high is a tower which casts a shadow 116.8 feet long?

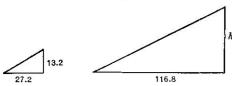


Fig. 20. 27.2 : 13.2 = 116.8 : h.

Problem 37. At 2,400 yards an increase of 1 mil in the elevation of a gun increases the range 25.0 yards. What change in elevation will increase the range 40 yards?

The mil is the unit of angle in the artillery. It is equal to \$\frac{1}{400}\$ of 360°.

Example: The effects of wind on a shell are approximately proportional to the velocity of the wind. At 3,000 yards for a 3-inch gun, a rear wind of 10 miles per hour increases the range 30.1 yards. (a) What wind will increase the range 42.8 yards? (b) What wind will decrease the range 68.5 yards?

Answer (a) Rear wind of 14.2 miles per hour. (b) Head wind of 22.8

miles per hour.

SQUARES

Example: Find the area of a square plot of ground measuring 128 yards on a side.

			<u> </u>		
	(K	Ludda	ւնորդայի	समामिक्क्ष्म	dittilititititiki rectari kurtuntuntun kuludun kuludun kuludun kuluturi.
,	A	1,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	ամական	3	լույլ և լույլ ան անանան այլ անհան անհան և այլ անհան անհան և այլ անհան և այլ անհան և այլ անհան և այլ անհան և այ
1	B	1 4b'.	5b" )	'.L' '	control data to glad Suntajuni nababababa Buntu da da da Sula da
	T	المالية المرادية	ىلى ئىلىلىد	1 1 1 1 1 1 1 1 1	
L	CI				
	) <sup>D</sup>	<u>i</u> i	2 1	3 4	5 6 7 8 9 2
		. histoidhidhidhidhidh	ក្រជាការប្រជាជាជា	<u>haibinhadadayla</u>	paspanjiatinajanganganganganganganganganganganganganga
					Fig. 21.

Using the face of the rule with scale A, set the indicator to 128 on D, Directly above on A find the square required, 164. To place the decimal point make a rough calculation.

(128)<sup>2</sup> is roughly (130)<sup>2</sup> or 16900. Then make 164 look like 16900 by placing the point as follows: 16400. The result is only correct to three figures. The complete result is 16384.

If greater accuracy is desired, a number may be squared by the use of the longer scales C and D.

Example: Find the square of 128.

Regard this as an example in multiplication equivalent to:

Find  $128 \times 128$ .

To 128 on D set left index.

Opposite 128 on C read 1638 on D.

Placing the decimal point by a rough calculation, the result is 16380.

Example: Square 652.

Set the indicator to 652 on D reading the square 425 on A. Notice that here the arithmetic square would be 425104, but on the slide rule we can get only the first three figures, 425. This, however, is close enough for most practical purposes, such as estimating on contract work.

To place the decimal point.

 $652^2 > 600^2 = 360000.$  $< 700^2 = 490000.$ 

since the value is between these limits the result is 425000.

Find the squares of the following numbers:

 Problem
 38.
 3.2
 Problem
 42.
 276.
 Problem
 46.
 .0057

 39.
 4.65
 43.
 34.2
 47.
 .0244

 40.
 1.12
 44.
 .66
 48.
 2240.

 41.
 8.65
 45.
 .0625

Example: Find the area of a circular plot of ground measuring 14.5 feet in diameter.

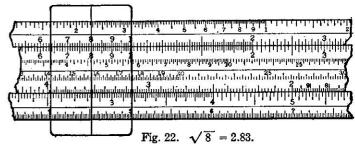
Use the formula  $A=.7854\ d^2$ , which means that the area of the circle is equal to .7854 multiplied by the square of the diameter. Set the indicator to 145 on D. The square is found directly above on A, but need not be read. Set the right-hand index of the slide to the indicator. Move the indicator to the constant, .7854 on B, and opposite find the result, 165 sq. ft. on A.

This constant, .7854, is so frequently used that it has been marked by a special line on the right-hand half of the A and B scales.

# SQUARE ROOTS

**Example:** How long must one side of a square garden bed be made in order that it shall contain 8 square yards?

Here we have to find the square root of 8.



Set the indicator to 8 on scale A. Assume that scale A runs from 1 to 100, so that 8 is found on the left-hand half of the rule.

Now under the hair line on scale D, find 2.83, the square root.

Then the result is 2.83 yards.

Example: Find  $\sqrt{3}$ .

Set the indicator to 3 on A.

Under the hair line find 1.73 on D.

Example: Find  $\sqrt{30}$ .

Set the indicator to 30 on A, being careful to notice that 30 is indicated by 3 on the right-hand half of the rule. Opposite the indicator on D, find 5.48.

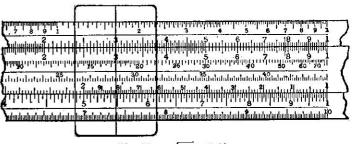


Fig. 23.  $\sqrt{30} = 5.48$ .

Example: Find  $\sqrt{300}$ .

Move the decimal point an even number of places in order to obtain a number that is between 1 and 100. This can be done by moving the point two places to the left, giving  $\sqrt{3.00}$ .

Find the  $\sqrt{3}$ , which is 1.73. Then move the decimal point half as many places as it was moved in the first place, but in the opposite direction. In this case, move the point in 1.73 one place to the right, giving 17.3.

Example: Find  $\sqrt{.30}$ .

Move the point two places to the right, obtaining 30.

Find  $\sqrt{30} = 5.48$ .

Move the point one place to the left, obtaining .548 for the result.

Example: Find  $\sqrt{.03}$ .

Move the decimal point two places to the right, obtaining  $\sqrt{3}$ .

Find  $\sqrt{3} = 1.73$ ,

Move the point one place to the left, obtaining .173.

Example: Find  $\sqrt{.003}$ .

Move the point four places to the right, obtaining  $\sqrt{30}$ .

Find  $\sqrt{30} = 5.48$ .

Move the point two places to the left, obtaining .0548.

Find the square roots of the following numbers:

Problem	49.	1.42	Problem 5	52.	.142	Problem	55.	.365
	50.	14.2		33.	2.43			.31416
	51.	142		54.	85.4		57.	1450

**Problem 58.** Make a list of square roots of whole numbers between 110 and 130.

**Problem 59.** On a baseball field, find the distance from home plate to second base, measured in a straight line. (The distance between the bases is 90 feet).

Problem 60. Water is conducted into a tank through two lead pipes having diameters of  $\frac{5}{8}$  and  $\frac{1}{4}$  inches, respectively. Find the size of the lead waste pipe that will allow the water to run out as fast as it runs in.

Use 5% and 134 in the decimal form.

Find 
$$\sqrt{(.625)^2 + (1.75)^2}$$
.

NOTE:—Perform the addition by arithmetic. The slide rule cannot be used to advantage in addition.

**Problem 61.** Two branch iron sewer pipes, each 6 inches in diameter, empty into a third pipe. What should be the diameter of the third pipe in order to carry off the sewage?

## TEST PROBLEMS

Read carefully the following instructions:

- a. Copy the test on your paper in the form given below.
- b. Work the problems straight through, setting down the answers in the column at the extreme right.
- c. Fold these answers underneath the paper.
- d. Work the problems through again, setting down the answers in the other column.
- e. Compare the two sets of answers.
- f. If the answers to any problem do not agree (within one point in the third place), work the problem again.
- g. The correct results are given on page 85.

# TEST

			Answers Second Time	Answers First Time	Credits
<b>Problem</b>	62.	$1.28 \times 2.46$			20
"	63.	84 ÷ 59.5			20
"	64.	$\frac{58.5 \times 15.2}{78}$			20
44	65.	6.25:24.2=9.5:			20
**	66.	$\sqrt{182}$			20

# CHAPTER II

# THEORY OF THE SLIDE RULE

# HISTORICAL NOTE

In 1614 John Napier, of Merchiston, Scotland, first published his "Canon of Logarithms.'

Napier concisely sets forth his purpose in presenting to the world his system

of Logarithms as follows:

Seeing there is nothing (right well beloved Students of Mathematics) that is so troublesome to mathematical practice, nor doth more molest and hinder calculators, than the multiplications, divisions, square and cubical extractions of great numbers, which besides the tedious expense of time are for the most part subject to many slippery errors, I began therefore to consider in my mind by what certain and ready art I might remove those hindrances.'

Napier builded better than he knew. His invention of logarithms made possible the modern slide rule, the fruition of his early conception of the

importance of abbreviating mathematical calculations.

In 1620 Gunter invented the straight logarithmic scale, and effected

calculation with it by the aid of compasses.

In 1630 Wm. Oughtred arranged two Gunter logarithmic scales adapted to slide along each other and kept together by hand. He thus invented the first instrument that could be called a slide rule.

In 1675 Newton solved the cubic equation by means of three parallel logarithmic scales, and made the first suggestion toward the use of an indicator.

In 1722 Warner used square and cube scales.

In 1755 Everard inverted the logarithmic scale and adapted the slide rule to gauging.

In 1815 Roget invented the log-log scale.

In 1859 Lieutenant Amèdèe Mannheim, of the French Artillery, invented the present form of the rule that bears his name.

In 1881 Edwin Thacher invented the cylindrical form which bears his name. In 1891 Wm. Cox patented the Duplex Slide Rule. The sole rights to

this type of rule were then acquired by Keuffel & Esser Co.

For a complete history of the Logarithmic Slide Rule, the student is referred to "A History of the Logarithmic Slide Rule," by Florian Cajori, published by the Engineering News Publishing Company, New York City. This book traces the growth of the various forms of the rule from the time of its invention to 1909.

## ACCURACY

The accuracy of a result depends upon (a), accuracy of the observed data; (b), accuracy of mathematical constants; (c), accuracy of physical constants; (d), precision of the computation.

# ACCURACY OF THE OBSERVED DATA

The precision of a measurement is evidently limited by the nature of the

instrument, and the care taken by the observer.

Example 1. If a distance is measured by a scale whose smallest subdivision is a millimeter, and the result recorded 134.8 mm., evidently the result is correct to 134, but the .8 is estimated. Hence it is known that the actual measurement lies between 134 and 135 and is estimated to be 134.8.

The result 134.8 is said to be "correct to four significant figures."

If the result were desired correct to only three figures, it would be recorded 135, since 134.8 is nearer 135.0 than 134.0. This result is said to be "correct

to three significant figures."

Example 2. If the distance is measured by a rule whose smallest subdivision is .1 inch, and found to be exactly 8. inches, the result would be recorded 8.00 inches. The zeros record the fact that there are no tenths and no hundredths, but the distance is exactly 8 inches. The result, 8.00 inches, is said to be "correct to three significant figures."

Example 3. If an object is weighed on a balance capable of weighing to .01 gram, then .001 gram can be estimated. Suppose several objects are weighed, with the following results:

1.	Seven grams	recorded	7.000	grams
2.	Seven and a half grams	"	7.500	"
3.	Seven and 9/100 grams	**	7.090	"
4.	Seven and 6/1000 grams	3 "	7.006	66
5.	4/100 and $2/1000$ grams	**	.042	**

Note that readings with the same instrument should show the same number of places filled in to the right of the decimal point, even if zero occurs in one or all of these places.

In number 5, the result, .042 grams is said to be "correct to two significant figures." The first significant figure is 4 and the second is 2.

Example 4. When we say that light travels 186,000 miles per second, we mean that the velocity of light is nearer 186,000 miles than 185,000 miles, or 187,000 miles. The result is said to be "correct to three significant figures,"

Summarizing the preceding examples:

Example 1. 134.8 is correct to four significant figures.

Example 2. 8.00 is correct to three significant figures.

Example 3. .042 is correct to two significant figures.

Example 4. 186,000. is correct to three significant figures.

Counting from the left, the first significant figure is the first figure that is not zero.

After the first significant figure, zero may count as a significant figure, as in Example 2, where it represents an observed value; or it may not so count, as in Example 4, where the zeros merely serve to place the decimal point correctly, the number 186,000, being correct only to the nearest thousand miles.

Similarly in results derived from calculation, zero counts as a significant figure if it represents a definite value, e. g.  $25 \times 36 = 900$ .

Both zeros in 900 are significant figures. On the other hand, zero is not a significant figure if it does not represent a definite value, but merely serves to place the decimal point.

Find the cube of 234.

The complete result is 12,812,904.

On the slide rule only the first three significant figures can be found, and the result is 12,800,000. Here 128 are significant figures and the five zeros following are not significant, since they do not represent definite values, but merely serve to place the decimal point.

As far as calculation on the slide rule can determine, each of these five zeros might be any one of the numbers from 0 to 9. Arithmetical calculation shows that they are really, 12,904.

#### ACCURACY OF MATHEMATICAL CONSTANTS

A mathematical constant may be carried to any desired degree of accuracy, e. g., the value of  $\pi$  usually given as 3.14159 has been calculated to 707 decimal places. For ordinary calculations 3.14 or 34 is sufficiently accurate.

# ACCURACY OF PHYSICAL CONSTANTS

Most physical constants are only correct to three significant figures and some only to two figures.

e. g., The weight of a cu. ft. of water is 62.5 lb.

The weight of a cu. in. of cast iron is .26 lb.

# LIMITS OF ACCURACY

Holman's rule states that if numbers are to be multiplied or divided, a given percentage error in one of them will produce the same percentage error in the result.

In other words, a chain is no stronger than its weakest link.

Since physical constants are not usually correct beyond three significant figures, and the observed data in an experiment are rarely reliable beyond this point, the slide rule reading to three figures gives results sufficiently accurate for most kinds of practical work.

#### PERCENTAGE OF ERROR

If a result is correct to three significant figures, the ratio of the error to the result is less than 1:100.

Suppose, for example, the result is 3527.6, which is known to be correct to three significant figures. Then the figures 352 are known to be correct and the figures 7.6 are doubtful.

Since 7.6 is less than 10 and 3527.6 is greater than 1000, the error must be less than 10:1000 or 1:100.

$$\frac{7.6}{3527.6} < \frac{10}{3527.6} < \frac{10}{1000}$$
, or  $\frac{1}{100}$ .

A result read on the 10-inch slide rule to four significant figures is 1324, which is correct to three figures, 132, while the fourth figure, 4, is a close estimate not more than one point away from the correct reading.

The error here is less than  $\frac{1}{1324}$ , which is less than  $\frac{1}{1000}$ . Hence the error in this reading is less than one-tenth of one per cent.

It is evident that the per cent of error holds throughout the length of the slide rule, since the first significant figure increases from 1 to 10 as spaces decrease.

e. g., On the right end of the rule, a result read 998 might be really 999 making an error of 1 in 999 or approximately  $\frac{1}{1000}$  or  $\frac{1}{10}$  of 1%.

If greater accuracy is desired, a twenty-inch rule will give results correct to within one part in two thousand; while the Thacher Cylindrical Rule will give results correct to within one part in ten thousand.

# LOGARITHMS

 $10^2 = 100.$ 

Another form of making this statement is:

The logarithm of 100 is 2.

In the same way,  $10^3 = 1,000$ 

or the logarithm of 1,000 is 3.

From these examples it is evident that the logarithm is the exponent which is given to 10.

Fill out the blanks in the following table:

$$10^4 = 10,000$$
 Log  $10,000 = 10^5 = 100,000$  Log  $100,000 = 10^1 = 10$  Log  $10 = 100,000 = 100 = 100$  Log  $10 = 100$  Log  $10 = 100$ 

# LAW OF MULTIPLICATION

$$10^2 = 100.$$

$$10^3 = 1,000.$$

$$10^2 \times 10^3 = 100 \times 1,000.$$

$$10^5 = 100,000.$$

Log 100,000 is 5.

Since 5 is the sum of 2 and 3,  $\log 100,000 = 2 + 3 = \log 100 + \log 1,000$ , or

The logarithm of a product is the sum of the logarithms of the multiplicand and the multiplier.

Hence to multiply one number by another, add their logarithms.

The construction of the rule allows this addition to be done easily.

The scales are divided proportionally to the logarithms of the numbers.

If the scale is considered as divided into 1,000 units, then any number—1, 2, 3, etc.,—is placed on the rule so that its distance from the left index is proportional to its logarithm.

Since  $\log 1 = 0$ , 1 is found at the extreme left.

"  $\log 2 = .301$ , 2 is found 301 units from the left.

" log 3 = .477, 3 " " 477 " " "

" log 9 = .954, 9 " " 954 " " "

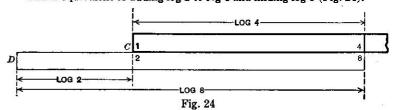
" log 10 = 1.000, 10 " " 1000 " "

On the scale the number 8 is placed three times as far from the left index as 2, because the logarithm of 8 is three times the logarithm of 2.

## MULTIPLICATION

When we multiply 2 by 4, we set the left index of the slide to 2 on scale D and under 4 on scale C find the product, 8 on scale D.

This is equivalent to adding log 2 to log 4 and finding log 8 (Fig. 24).



Example: Multiply 2.45 by 3.52.

Opposite 2.45 on D, set 1 on C and under 3.52 on C find 862 on D.

Roughly calculating,  $2.45 \times 3.52 = 2 \times 4 = 8$ .

Hence, we place the decimal point to make the result as near 8 as possible; and the result is 8.62.

Example: Multiply 24.5 by 35.2.

Working this like the preceding example, without regard to the decimal point, we obtain 862.

Roughly calculating,  $24.5 \times 35.2 = 25 \times 36 = 900$ .

Placing the decimal point to make 862 as near 900 as possible, we obtain 862.

Example: Multiply 6.234 by 143.

Taking 6.234 correct to three significant figures we multiply 6.23 by 143

Opposite 623 on D set 1 on C.

Under 143 on C find 891 on D.

Roughly calculating,  $6 \times 140 = 840$ .

Therefore the result is 891.

Example: Multiply 2.46 by 7.82.

Method I.

When the product of the given numbers is greater than 10, the sum of their logarithms will exceed the length of the rule. Hence if we set the left index of the slide to 246 on D, the other number 782 on C projects beyond the rule. In this case, think of the projection as wrapped around and inserted in the groove at the left, which would be the case in a circular slide rule. Now the right and left-hand indexes coincide.

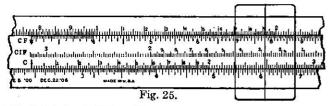
Hence set the right index of the slide to 246 on D.

Under 782 on C find 192 on D.

Roughly calculating,  $2 \times 8 = 16$ ,

Hence the result is 19.2.

Method II. By the use of the folded scales, CF and DF, the product of any two numbers may be found without any uncertainty regarding the index, provided that at least half of the slide remains in the groove.



Set the left index to 246 on D.

Since 782 on C is beyond the right-hand end of the rule, set the indicator to 782 on CF and read the product opposite the indicator on DF.

The result is 19.2.

Example: Multiply .146 by .0465.

Opposite 146 on D set 1 on C.

Under 465 on C, find 679 on D.

Roughly calculating,  $.1 \times .05 = .005$ .

Hence the result is .00679.

Find the value of

Problem 67.  $2.34 \times 3.16$ . 70-  $8.54 \times 6.85$ . 73.  $.023 \times 2.35$ .

**68.**  $3.76 \times 5.14$ . **71.**  $34.2 \times 7.55$ . **74.**  $.00515 \times .324$ .

**69.**  $1.82 \times 4.15$ , **72.**  $4.371 \times 62.47$ , **75.**  $.00523 \times .0174$ .

**Problem 76.** Find the circumferences of circles having diameters of 4 ft., 6.5 ft., 14 ft.

Opposite  $\pi$  on A, set 1 on B.

Above 4, 6.5, and 14 read the circumferences on A.

Or opposite 4, 6.5, and 14 on C, read the circumferences on CF; in which case the results can be read to an additional significant figure, as 12.56.

## DIVISION

In division, reversing the operation of multiplication,

 $8 \div 4 = 2$ . (See Fig. 24)

We subtract log 4 from log 8 and obtain log 2.

## The Use of Scales CF and DF

The folded scales, CF and DF, were devised to eliminate the number of re-settings of the slide which result where only one straight scale with consecutive graduations is employed.

These folding scales have been split at  $\pi$ , since this is a useful constant; and by splitting the scale at this point the 1 or index is thrown near the middle of the rule.

The examples which follow bring out clearly the advantages of the folded scales.

**Example:** Find the value of  $3 \times 5$ .

To 3 on D set the left index of C.

Over 5 on CF find 15 on DF.

**Explanation:** Since we are measuring the result on DF, we have at the start,  $\log \pi$  at the left end of DF.

When we set the left index of the slide to 3, we increase  $\log \pi$  by the addition of  $\log 3$ .

When we move the indicator to 5 on CF, we increased (log  $\pi + \log 3$ ) by the addition of (log 5 — log  $\pi$ ).

The sum of these logs gives

 $\log \pi + \log 3 + \log 5 - \log \pi = \log 3 + \log 5 = \log 15$ .

This example shows how multiplication may be performed by the use of D, CF and DF when it would have required a re-setting of the slide if we had first tried the left index, then the right index and used only scales C and D.

This is especially valuable when one factor is a constant, as in the following example.

**Example:** Convert into centimeters:

1. 2.07 inches.

2. .858 inches.

3. 3.14 inches.

4. 6.83 inches.

Since 1 inch = 2.54 centimeters,

To 2.54 on D set the left index of C.

1. Under 2.07 on C find 5.25 on D.

Order 2.07 on C find 5.25 on D.
 Over 858 on CF find 218 on DF.

Placing the decimal point by inspection, we have 2.18.

3. Under 3.14 on C, find 7.97 on D.

4. Over 6.83 on CF, find 173 on DF.

Placing the decimal point by inspection, we have 17.3. After working I without the use of CF and DF, it would have been necessary to re-set the slide using the right index. Scales CF and DF save time in such operations as this.

Care should be taken to keep at least half of the slide in the groove, using the right or left index, as the case requires.

EXAMPLE: Find the circumference of a circle having a diameter of 2".

Set the indicator to 2 on D.

On DF, opposite the indicator, find 6.28.

Since  $\pi$  on DF is opposite 1 on D, scales D and DF furnish a table of circumferences and corresponding diameters, a diameter D on having its circumference directly above it on DF.

Example: With only one setting of the slide, find the following products:

1.  $.26 \times 3.5$ . Answer .91.

2. .25  $\times$  5.6. (Without re-setting the slide, opposite 5.6 on CF read 1.456 on DF.)

3.  $.26 \times 1.12$ . Answer .291.

4.  $.26 \times 8.4$ . Answer 2.18.

Find the circumferences of circles having the following diameters:

5. 2.14 in. Answer 6.72 in.

6. 7.8 ". Answer 24.5 ".

7. 4.35 ". Answer 13.7 ".

8. 6.2 ". Answer 19.47".

# PROPORTION

Problems in proportion are special cases of multiplication and division.

**Example:** Solve 16:27=17.5:x.

$$x=\frac{27\times1.75}{16}$$

Following the method on page 13, Fig. 14, we first divide 27 by 16 by setting 16 on C to 27 on D. We have subtracted the logarithm of 16 from the logarithm of 27. The result of this division, which is 169, is found on D under the left index. Now multiply by 17.5 by moving the indicator to 175 on C. On D, opposite the indicator, read 295.

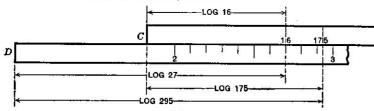


Fig. 26.

To place the decimal point, note that 16 has the same relation to 27 that 17.5 has to x. Since 27 is not quite twice 16, x will be not quite twice 17.5. Hence the decimal point must be placed so that the answer is 29.5.

The method of working a proportion is easily remembered as follows:

$$\begin{array}{cccc}
C & D & C & D \\
16 : 27 & = 17.5 : x.
\end{array}$$

**Example:** Solve x:24 = 11:18.

$$C D C D 
x: 24 = 11: 18.$$

To 18 on D, set 11 on C. Opposite 24 on D find x on C.

The significant figures of x are 147.

To place the decimal point, note that since 11 is a little more than half of 18, x will be a little more than half of 24, or 14.7.

# SQUARES AND SQUARE ROOTS

$$(10^3)^2 = 10^2 \times 10^3$$
.  
= 10°.  
Since 6 = 2 × 3,  
Log  $(10^3)^2 = 2 \times \log 10^3$ .

Hence, to square a number, multiply its logarithm by 2.

The space given to each number on scale D is twice that given to the same number on scale A.

As an example, suppose we wish to square 3.

This can be done by doubling the space given to 3 on scale A and finding 9, or looking for 3 on scale D and finding its square above it on scale A.

Reversing the operation gives the square root.

As an example, find the square root of 9.

Look for 9 on scale A, and directly below it on D find 3, its square root.

# CUBES AND CUBE ROOTS

 $(10^2)^3 = 10^2 \times 10^2 \times 10^3$ . =  $10^6$ .

Since  $6 = 3 \times 2$ ,

 $Log (10^2)^8 = 3 \times log 10^3$ .

Hence, to cube a number, multiply its logarithm by 3.

Scale K is graduated from 1 to 1,000, while scale D runs from 1 to 10. The space given to each number on scale D is three times that given to the same number on scale K.

Example: Find the cube of 2.

This could be done as follows:

Find 2 on scale K with the indicator. We have now measured log 2, from the left end of the rule.

Measure off three times this space on scale K and we have the indicator set at  $\log 2^3$  or 8.

But this measuring can be done by setting the indicator to 2 on scale D, since the space given to 2 on D is three times that given to 2 on K.

Hence, to cube a number, using the face of the rule on which scale K appears, set the indicator to the given number on scale D.

On scale K, opposite the indicator, find the result which is  $2^3$ , or 8.

In the same way show that

Example:  $3^3 = 27$ . (Note that the reading is on the second of the K scales running from 10 to 100. This scale we will call  $K_2$ ).  $5^3 = 125$ . (Note that the reading is on the third of the K

 $6^3 = 125$ . (Note that the reading is on the third of the K scales running from 100 to 1,000. This scale  $7^3 = 343$ . we will call  $K_3$ .)

 $8^3 = 512.$ 

 $9^3 = 729.$ 

 $11^3 = 1331.$ 

Roughly calculating, we know 11<sup>3</sup> is a little larger than 10<sup>3</sup>, or 1,000. We also can see that the units figure will be the cube of 1, or 1. The mark on the rule gives 133. Hence the total result is 1,331.

In the same way, work the following:

Example:  $12^3 = 1,728$ .

Find the cubes of the following numbers correct to 4 significant figures:

Problem 77. Find the cube of 13. Problem 82. Find the cube of 18. 78. " " 14. 83. " " 19.

79. " " " 15. 84. " " " 20. 80. " " " 16. 85. " " " 21.

81. " " 17.

Find the cubes of the following numbers correct to 3 significant figures:

Example: Find the cube of 22.

(The complete answer is 10,648, but on the slide rule we get 10.600 correct to 3 significant figures. The error is less than one-half of one per cent).

" .057.

The state of the s

Problem 86. Find the cube of

46.

88. 47. (Set the right-hand index on the slide to 47 on D.)

89. 53.

Find the cube of Problem 90. 64. Problem 96. Find the cube of .342.

91, 758. 92. 44 232.

.0068. 93. 425.6.\* 44 " 1.03.

94. " 46 87.9. 100. " 2.12.

" 44 " 139.

\*In Problem 93, 425.6 is approximately 426. Roughly approximating the result  $400^3 = 64,000,000$ . The rule gives us 771. Hence the result is 77,100,000 correct to three significant figures. The complete result is 77,091,209.

Problem 101. How many gallons will a cubical tank hold that measures 26 inches in depth? (1 gal. = 231 cu. in.)

# CUBE ROOTS

Example: Find the cube root of 8.

Set the indicator to 8 on the left-hand K scale, called  $K_1$ . opposite the indicator, find 2.

Explanation. Log  $\sqrt[3]{8} = \frac{1}{9}\log 8$ .

Hence, to find the cube root of a number, divide the logarithm of the number by 3.

Using log 8 on scale D as a unit, set the indicator to 8 on D.

Measuring from the left index one-third of this space, we find 2 on scale D. But one-third of log 8 on D may be found by setting the indicator to 8 on the left-hand K scale, since each K scale is one-third as long as the D scale.

Example: Find  $\sqrt[3]{27}$ .

Set the indicator to 27 on the middle K scale, called  $K_2$ .

On scale D, opposite the indicator, find 3.

Example: Find \$\frac{3}{125}\$.

Set the indicator to 125 on the right-hand K scale, called K.

On scale D, opposite the indicator, find 5.

Example: Find  $\sqrt[3]{9}$ .

Set the indicator to 9 on  $K_1$ .

On D, opposite the indicator, find 208, the significant figures of the result. Placing the decimal point by inspection, we have  $\sqrt[3]{9} = 2.08$ .

Example: Find  $\sqrt[3]{90}$ .

Set the indicator to 90 on  $K_2$ .

On D, opposite the indicator, find 4.48, the cube root.

Example: Find \[ \sqrt{900}. \]

Set the indicator to 900 on  $K_1$ .

On D, opposite the indicator, find 9.66, the cube root.

Example: Find  $\sqrt[3]{.9}$ .

Point off the number into periods of three figures each, counting from the decimal point, adding zeros to fill out the three figures. This gives .900. Now we have the problem of finding the cube root of 900 as in the previous example.

The significant figures are 966, the setting of the indicator being the same as in the previous example.

In placing the decimal point, there is a decimal place in the cube root for every decimal period of three figures in the given problem.

Given number .900,000,000.

Cube root

9 6 6

The result is .966.

Example: Find \$\sqrt{0.09}.

Following the plan of the previous example, the first decimal period is .090.

Finding  $\sqrt[3]{90}$  as before we have 448 for the significant figures. Hence, the result is .448.

# Rule for placing the decimal point in Cube Root

From a consideration of the preceding eight examples, we derive a rule for placing the decimal point in finding the cube root of numbers that do not lie between 1 and 1,000.

- a. Move the decimal point 3, 6, or 9 places, as may be necessary, in either direction to obtain a number between 1 and 1,000.
  - b. Find the cube root of this new number using

 $K_1$  for a number of one integer,

 $K_{2}$  " " two integers,  $K_{3}$  " " three integers.

c. In the result, move the decimal point one third as many places as it was moved in a, and in the opposite direction.

Example: Find  $\sqrt[3]{56,342}$ .

- a. Move the decimal point three places to the left, obtaining 56.342.
- b. Find the cube root of 56.3 which is 3.83.
- c. Move the decimal point one place to the right, obtaining 38.3.

Example: Find  $\sqrt[3]{.00382}$ .

- a. Move the decimal point three places to the right, obtaining 3.82
- Find the cube root of 3.82 which is 1.563.
- c. Move the decimal point one place to the left, obtaining .1563.

roblei	n				Proble	m		*(6	
102.	Find t	the cube	root of	3.	112.	Find th	ie cube	root	of 50.
103.	"	**	**	30.	113.	44	"	**	7.35
104.	**	46	"	300.	114.	**	**	ш	.575.
105.	**	4	"	.3.	115.	16	"	46	241.
106.	"	**	**	.03.	116.	**	"	"	3840.
107.	**	**	44	.003.	117.	4.4	"	"	52076.
108.	**	46	46	2613.	118.	44	***	46	.0163.
109.	"	"	**	47.8.	119.	**	"	46	.0094.
110.	44	46	44	.784.	120.	46	44	44	1.036.
111.	"	16	46	45083.	121.	"	"	"	108723

Problem 122. How deep should a cubical box be made in order to contain 8,500 cubic inches?

# MULTIPLICATION OF MORE THAN TWO NUMBERS

Using only scales C and D.

**Example:** Find the value of  $4.1 \times 56 \times .26 \times .49$ .

Using scales C and D, set the right index on C to 41 on D and move the innicator to 56 on C. We have now multiplied 41 by 56. The result thus far found on D, opposite the indicator is 2296, without regard to the decimal point.

Now set the left index of C to the indicator and move the indicator to 26 on C, thus adding the log of 26 to the former result. On D under the indicator is 597.

Set the right index to the indicator and move the indicator to 49 on C. On D opposite the indicator, find 2925.

The position of the decimal point is determined by a rough calculation.

$$4.1 \times 56 \times .49$$
 is, roughly,  $4 \times 60 \times + \frac{1}{4} \times .5 = 30$ .

Placing the decimal point so as to make 2925 read as near 30 as possible, it is evident that the result is 29.25.

Find value of

Problem |23.7.1 
$$\times$$
 31  $\times$  .42 | Problem |26. | 8.25  $\times$  .036  $\times$  1.07  $\times$  4.12 | 124. | .64  $\times$  32  $\times$  5.6 | 127. | 6.2  $\times$  37.8  $\times$  .0052  $\times$  46 | 125. | 16.3  $\times$  1210  $\times$  3.65  $\times$  243

On the Polyphase-Duplex Rule the operations in these problems may be considerably abridged by the method of pages 33 and 34.

# THE USE OF SCALES CI AND CIF

Important improvements found on the Polyphase Duplex Slide Rule are the inverted scales CI and CIF.

These scales enable reciprocals of all numbers to be read at once without setting the slide. They also allow three factors to be taken at a single setting, thus saving one or more settings in many formulas, and increasing both speed and accuracy.

Scale CI (or C inverted) is like scale C, except that the numbers are placed on the rule in inverted order. Reading from left to right, the numbers on C run from 1 to 10, while those on CI run from 10 to 1.

Scale CIF is like scale CI, except that on CIF the number 1 is near the middle of the rule.

In the following problems, the combination of scales is selected that will keep at least half of the slide within the groove. This arrangement makes it possible to multiply any three factors together with only one setting of the slide.

# RECIPROCALS

Two numbers are reciprocals if their product is equal to 1, or we may say that the reciprocal of a number is 1 divided by that number.

e. g. 5 and 1/5 are reciprocals since  $5 \times 1/5 = 1$ .

To find the reciprocal of a number:

Set the indicator to the given number on scale C.

Opposite the indicator on scale CI will be found the significant figures of the reciprocal.

The decimal point is placed by inspection.

An easier method is to set the indicator to the given number on scale CF.

Opposite the indicator on scale CIF will be found the significant figures of the reciprocal.

Since both CF and CIF are on the slide, no setting of the indexes is necessary.

Example. Find the reciprocal of 2.

Set the indicator to 2 on C. Opposite the indicator on CI, find 5.

Placing the decimal point by inspection, the result is .5.

The same result can be found more rapidly by moving the indicator to 5 on CF and reading the result directly on CIF.

Example: Find the reciprocal of .236.

Set the indicator to 236 on C.

On CI, opposite the indicator, find 424.

Roughly calculating 1/.236 = 1/.2 = 5.

Hence the result is approximately 5 or 4.24.

The same result can be found more rapidly by moving the indicator to 236 on CF and reading the result directly on CIF.

Find the reciprocals of the following numbers:

Problem	128.	7.2	Problem 133.	.182.
	129.	.41	134.	56.5
	130.	37.8	135.	.85
81	131.	68.2	136.	7.35.
	132	073	137	0063

#### MULTIPLICATION

**Example:** Multiply 3 by 2, using the scale CI.

Set the indicator to 3 on D.

To the indicator set 2 on CI.

Opposite the right index find 6 on D, or opposite 1 on CIF find 6 on DF.

Note that 3 on Scale CI is also in alignment with 2 on Scale D. Hence, we may set the indicator to 2 on D. To the indicator set 3 on CI. Opposite the right index find 6 on D.

Explanation

log 3	+	log 2	$= \log 6.$		
measured on D		measured on CI or CIF.	$\begin{array}{c} \text{measured on } D \\ \text{or } DF. \end{array}$		

**Example:** Multiply 3 by 5, using the scale CI.

Set the indicator to 3 on D or DF.

To the indicator set 5 on CI or CIF.

Opposite the left index, find 15 on D, or opposite 1 on CIF find 15 on DF.

Work Problems 67 to 75—on page 24, using scales CI and CIF; and compare with the previous method of using the C and D scales alone.

# DIVISION

Example: Divide 28 by 7, using the inverted scale.

To 28 on Scale D set left index.

Set indicator to 7 on CI.

Opposite indicator on scale D read 4.

Or:

To 28 on Scale D set right index.

Set indicator to 7 on CIF.

Opposite indicator on Scale DF read 4.

# SUCCESSIVE DIVISION.

The inverted scale is useful in problems of the type  $x = \frac{a}{u}$ , where a is a

constant and y assumes successive values.

Example: A field rheostat on an electric generator is used to vary the resistance so as to give it the following values in ohms: 250, 298, 347, 401,

If the voltage is 125, what are the values of the field current?

R (Varying)

where I is the current in amperes; E, the electromotive force in volts; and R, the resistance in ohms.

$$I = \frac{125}{250}$$
,  $\frac{125}{298}$ ,  $\frac{125}{347}$ ,  $\frac{125}{401}$ ,  $\frac{125}{453}$ ,  $\frac{125}{496}$ 

To 125 on D set 10 on CI (left index), or to 125 on DF set 1 on CIF. Opposite 250 on CI or CIF, read .500 on D or DF.

.312 " " " " 453 " " " " " .276 " " " " 496 " " " " " .252 " " " "

From one setting of the slide, all six values are read. By the use of Scales C and D alone, six settings of the slide would have been required.

# THREE FACTORS

$$a \times b \times c = x$$

Method I. Using CI.

To a on D, set b on CI.

a. At c on CF read x on DF.

or b. At c on C read x on D.

Example:  $2 \times 3 \times 7 = x$ .

To 2 on D set 3 on CI.

At 7 on CF read 42 on DF.

S	To the contract of the contrac
	- Shiridan (Antaland), artura faritan faritan karina kabadi abada kabada abada abar artura tara tara tara tara
անություն առափուն մետևում գ	ការតាមការក្រាលការស្រាស់មានស្រាស់មានស្រាស់មានប្រជាជាក្នុងការប្រជាជាក្នុងការប្រជាជាក្នុងការប្រជាជាការប្រជាជាការប
Manufacture Indicates	<del>րա իրգի որ են ակեր այն արև բարարարարի հերև իր երև իրև իրև իրև իրև իրև իրև իրև իրև իրև ի</del>
KEUPPE & CORE C	M.T. PAT JUNE 5 '00 DEC 22'00 MADE MUSA
	Fig. 27.

Explanation

log 2 log 3 log 7 log 42.

measured on Dmeasured on CI measured on CF

measured on DF

Note that this result is obtained with only one setting of the slide; and with no uncertainty as to whether the right or left index should be read. When the C and D scales alone are used, two settings of the slide are required, involving some uncertainty as to which index to use in steps 1 and 3.

Example:  $2 \times 3 \times 4 = x$ .

To 2 on D, set 3 on CI. At 4 on C, read 24 on D.

Try this example by Method Ia, following the directions given in the Example and note that the third factor, 4, on CF is beyond the end of the rule, Hence, instead of using CF and DF, we use C and D.

Explanation

log 2 log 24. log 3

measured on Dmeasured on CI measured on C measured on D

Method II. Using CIF.

To a on DF, set b on CIF.

a. At c on CF, read x on DF.

or b. At c on C read x on D.

Example:  $1.2 \times 1.2 \times 2 = x$ .

If we follow Method 1, the third factor, 2, is beyond the end of the rule both on scales CF and C.

By Method II.

To 1.2 on DF, set 1.2 on CIF.

At 2 on CF, read 2.88 on DF.

or at 2 on  $\hat{C}$ , read 2.88 on D.

Explanation

log 2.88 log 1,2 log. 1.2 log 2

measured on DF measured on CIF measured on CF or C measured on DF or D

Example:  $.75 \times a \ (= 6.4)$ 

To 72 on D, set 75 on C. Opposite any value of a, say 64, on CI or CIF, read 15 on D or DF. The decimal point of the result can be placed by inspection.

Note that when the C and D Scales alone are used in solving problems of this type, two settings will be required, including a separate setting for each value of the variable (a) of the denominator; whereas by employing the CI and CIF scales also, a single setting of the slide permits a solution for all values of the variable (a).

Using scale CI, find the value of:

Problem 141.  $.53 \times 42 \times 1.6$ Problem 138.  $6.1 \times 24 \times 8.2$ 142.  $54.3 \times 1.26 \times 2.3$ 139.  $6.1 \times 24 \times .32$ 

140.  $.53 \times 42 \times 6.5$ 

Using scale CIF, find the value of:

Problem 145. 6.25 × 9.5 × 1.5 " 146. 6.25 × 9.5 × 1.8 Problem 143.  $1.3 \times 1.5 \times 2.1$ 

144.  $6.1 \times 8.5 \times 2.5$ 44

147. Find the area of a circle whose radius is 4.5 ft.

(Use the formula  $A = \pi r^2$ , and arrange the slide rule work in the form:  $r \times r \times \pi$ 

Set r on CIF to r on DF, read area at right index of CF on DF.

Another method is to set the left index of the slide to 4.5 on D of the "K" face of the rule. Opposite  $\pi$  on B read 63.6 on A.

For multiplication and division of four numbers, one of which is  $\pi$ , see page 77.

# Four Factors

**Example:**  $1.43 \times 5.12 \times 1.76 \times 0.725 = x$ .

Method I.

Set indicator to 143 on D.

To indicator set 512 on CI. Ans. 7.32 on D opp. rt. endix. Indicator to 176 on C. Ans. 12.89 on D opp. indicator.

Set 725 on CI to indicator.

Opposite right index, read 934 on D.

This method requires only two settings of the slide.

**Method II.** Using only scales C and D.

1. Set left index to 143 on D.

Move indicator to 512 on C. Ans. 7.32 on D opp. indicator.

Set right index to indicator.

Indicator to 176 on C. Ans. 12.89 on D opp. indicator.

5. Left index to indicator.

6. Opposite 725 on C read 9.34 on D.

This method involves three settings of the slide, and some uncertainty as to which index to use in steps 1 and 3. Hence Method I will save considerable time in the solution of problems of this type.

# **Five Factors**

Example:  $2 \times 3 \times 4 \times 5 \times 6 = x$ .

To 2 on D set 3 on CI.

Indicator to 4 on C.

Set 5 on CI to indicator.

Opposite 6 on C, read 72 on D.

Placing the decimal point, the result is 720.

Note that the five factors are handled with only two settings of the slide. Without the CI scale, four settings of the slide would be required.

Occasionally in finding the product of three or more numbers, using scale CI, it would be necessary to re-set the index if the folded scales DF and CF were not present.

Example:  $2 \times 3 \times 1.3 = x$ .

To 2 on D. set 3 on CI.

Since 1.3 on C is beyond the left end of the rule. Move indicator to 10 on C.

Set 1 on C to the indicator.

Opposite 1.3 on C, read 7 8 on D.

One setting of the slide can be saved thus:

To 2 on D, set 3 on C1.

Opposite 1.3 on CF read 7.8 on DF, and CIF.

Using scales CI and CIF, fine the value of:

 $0.75 \times 1.1 \times 6.5 \times 8.65$ 

149.  $8.2 \times 0.45 \times 6.4 \times 16$ 150.  $16.3 \times 3.65 \times 243 \times 1210$ 

 $8.25 \times .036 \times 1.07 \times 4.12$ 151.

152.  $37.8 \times .0052 \times 46 \times 6.2$ 153.  $6.3 \times 2.5 \times .17 \times 5.4 \times 3.4$ 

**Example:** Solve  $x = \frac{\sqrt{78}}{y}$ , where y has the series of values, 1.2, 2.4, 3.6 4.8 and 9.0.

Set right index to 78 on scale A; opposite any value of y on scale CI, read x on D; or opposite any value of y on sale CIF read x on DF.

when 
$$y = 1.2$$
  $x = 7.36$ . Answer.  $3.68$   $3.6$   $2.45$   $4.8$   $1.84$   $9.0$   $9.81$ 

The last answer is read on DF opposite 9 on CIF, since 9 on CI is off the scale. The presence of the folded scale saves one setting of the slide.

Example: Solve  $x = \frac{y}{\sqrt{2\pi}}$ 

Set 2.7 on scale B to index.

Opposite any value of y on scale C read x on D.

**Example:** Find the value of  $4.3\sqrt[3]{25}$ .

Using indicator: to 25 on scale  $K_2$ , set 4.3 on scale CI.

At index read 12.57, the result, on D. Example: Find the value of  $\sqrt[3]{760}$ 

To 760 on  $K_3$  set 94 on C.

At index of CF (at middle of scale) find .0973 on DF.

The decimal point may be placed by inspection. The cube root of 760 has one integer, roughly 9; which divided by 90, shows the magnitude of the answer.

Example: Solve  $x = \frac{.27}{\sqrt[3]{.069}}$ 

Set indicator to 69 on  $K_2$ , Set 27 on scale C to indicator. At index on D read 658 on scale C.

Roughly calculating:

$$\frac{.27}{\sqrt[3]{.069}} = \frac{.28}{\sqrt[3]{.064}}$$
$$= \frac{.28}{.4}$$
$$= 7$$

Hence the result is .658.

Example: Solve  $x = 3\sqrt{23} \times \sqrt[3]{127}$ .

To 127 on  $K_8$  set 3 on scale CI.

Indicator to 23 on scale  $B_2$ ,

Opposite indicator on scale D, read 723.

Roughly calculating:

$$3\sqrt{23} \times \sqrt[3]{127} = 3 \times \sqrt{25} \times \sqrt[3]{125}$$
  
= 3 × 5 × 5.  
= 75.

Hence, the result is 72.3.

# CHAPTER III

# ADVANCED PROBLEMS

# COMBINED MULTIPLICATION AND DIVISION

Example: Find the value of

$$\frac{23.5 \times 45.3}{2670}$$

To 235 on D, set 267 on C. Opposite 453 on C find 399 on D. To obtain the decimal point make a rough calculation as follows:

$$\frac{23.5 \times 45.3}{2670}$$
 is roughly equal to  $\frac{20 \times 50}{3000} = \frac{1}{3}$ .

Hence, we must place the decimal point so as to make 399 approximately equal to ½. The result is evidently .399.

Another method of placing the decimal point:

$$\frac{23.5 \times 45.3}{2670} = \frac{(2.35 \times 10) \quad (4.53 \times 10)}{2.67 \times 1000}$$

$$= \frac{2.35 \times 4.53}{2.67} \times \frac{1}{10}$$

$$= 3.99 \times \frac{1}{10}$$

$$= 3.99$$

The first method will be found preferable, but may be checked by the second.

**Example.** Find the value of  $\frac{1.34 \times 2.15}{4.2}$ .

Method I. To 1.34 on D, set 4.2 on C.

Above 2.15 on CF, find 686 on DF.

Method I is preferable.

Method II. To 1.34 on D, set 4.2 on C. When we attempt to move the indicator to 2.15 on C, it is impossible, because 2.15 projects beyond the left end of the rule. Bring the indicator to 10 on C and move the slide so as to set the left index to the indicator. This divides by 10, but is permissible, since dividing by 10 does not change the order of significant figures. Now move the indicator to 2.15 on C; and on D, opposite the indicator, read 686. A rough calculation shows that:

$$\frac{1.34 \times 2.15}{4.2}$$
 is approximately equal to  $\frac{1 \times 2}{4} = \frac{1}{2}$ , or .5.

Hence, the result is .686.

Example. Find the value of

$$\frac{30.5 \times 50.6 \times 835}{3.64 \times 380 \times 42.5} = x.$$

$$\frac{D}{30.5 \times 50.6 \times 835} = \frac{D}{x.}$$

$$\frac{30.5 \times 50.6 \times 835}{3.64 \times 380 \times 42.5} = \frac{D}{x.}$$

The five operations are as follows:

Intermediate Results on D.

838, opposite right index.

At 305 on D set 364 on C.
 Move indicator to 506 on C.

424, opposite indicator.

3. Set 380 on C to the indicator.

111, opposite left index.

4. Indicator to 835 on C.

928, opposite indicator.

 Set 425 on C to the indicator, and opposite the index on C, find 218 on D.

Calculating roughly,

$$\frac{30\times50\times800}{3\times400\times40}=25.$$

Hence 218 must be made to look as near as possible like 25, giving the result 21.8. It is not necessary to obtain the intermediate results, but with beginners it is an advantage to check the work at every step.

Example: Find the value of

$$\frac{25.4 \times 570 \times 26.8 \times 8.63 \times 1.3}{1.55 \times 8350 \times 4.15 \times 2.24}.$$

$$D \quad C \quad C \quad C \quad D$$

$$\frac{25.4 \times 570 \times 26.8 \times 8.63 \times 1.3}{1.55 \times 8350 \times 4.15 \times 2.24} = x.$$

$$C \quad C \quad C \quad C$$
Intermediates on  $D$ 

$$At 254 on  $D$ , set 155 on  $C$$$

	1.	At 254 on D, set 155 on C	164
	2.	Move indicator to 570 on C.	934
	3.	Move the slide, setting 835 to indicator.	112
	4.	Indicator to 268 on C.	300
	5.	Move slide, setting $415$ on $C$ to indicator.	722
23	6.	Indicator to 863 on C.	625
	7.	Move slide, setting 224 to indicator.	279
	8.	Indicator to 13 on C.	363

Find the answer 363 on D opposite the indicator.

Calculating roughly:

$$\frac{25\times600\times30\times8\times1}{1\times8000\times4\times2}=60.$$

Making 363 look as much as possible like 60, we have 36.3.

Example: Find the value of

$$\frac{7.45}{3.65 \times .0267}$$

The preceding examples have had as many factors in the numerator as in the denominator or one more. This example can be changed to conform to these types by introducing unity as a factor in the numerator.

Method I. Using scales CI, C, and D.

- To 745 on D set 365 on C.
- Opposite 267 on CI read 764 on D.

Roughly calculating:

$$\frac{8 \times 1}{4 \times .02} = \frac{2.00}{.02} = 100.$$

Making 764 look as much as possible like 100, the result is 76.4.

The method is preferable, since it requires only one setting of the slide.

Method II. Using only scales C and D.

$$\frac{7.45}{3.65 \times .0267} = \frac{D \quad C}{7.45 \times 1} = x.$$

Check by

Intermediates on D.

1. Divide 7.45 by 3.65.

204, opposite left index.

2. Move indicator to 1 on C.

204, opposite indicator.

3. Move slide, setting 267 to indicator.

764, opposite right index.

Example: Find the value of

 $\frac{1}{2.34 \times .33 \times 5.25}$ 

Check by

Intermediates on D

1. To 1 on D, set 234 on C.

427, opposite right index.

2. Indicator to 33 on CI.

1295, opposite indicator.

3. 525 on C to indicator.

2467, opposite right index.

Rough calculation:

$$\frac{1}{2 \times \frac{1}{4} \times 6} = \frac{1}{4} = .25.$$

Making 2467 look as much as possible like .25 the result is .2467.

Example: Find the value of:

$$\sqrt{\frac{21.4 \times 3.45 \times 640}{4.15 \times .75 \times .08}}$$

Method I.—Work the example without regard to the square root, then find the square root of the result.

Method II.—Using scales A and B:

$$\frac{A \quad B \quad B}{21.4 \times 3.45 \times 640} = \frac{D}{x}.$$

$$\frac{4.15 \times .75 \times .08}{B} = \frac{D}{x}.$$

Intermediate on A.

1. To 21.4 on A set 4.15 on B.

516, opposite index.

Be careful to use 21.4 on the right half of A and not 2.14 on the left half, since the square root of 21.4 has different significant figures from the square root of 2.14. For the same reason use 4.15 on the left half of B.

- 2. Indicator to 3.45 on B (left half of rule)
- 178, opposite indicator.
- 3. Move slide setting .75 (right half) to indicator. 237, opposite index.
- 4. Indicator to 6.4 (left half) on B.

152, opposite indicator.

Change 640 to 6.4, by moving the decimal point an even number of places, in order not to change the square root.

- 5. Move slide setting 8 (left half) on B to indicator. 190, opposite index.
- 6. Opposite right index of B find 436 on D.

Rough calculation

$$\sqrt{\frac{20 \times 3 \times 600}{4 \times 1 \times .1}} = \sqrt{90000} = 300.$$

Placing the decimal point so as to make 436 as near as possible to 300, the result is 436.

Example: Find the value of  $\frac{254 \times 65 \times 24}{155 \times 45}$ .

Intermediate Results

- 1. Opposite 254 on *D*, set 155 on *C*.
  - 164. Opposite left index on D.
- 2. Move indicator to 65 on CF.

1065, Opposite indicator on DF.

3. Set 45 on CF to indicator.

237 On DF, opposite middle index (10)

4. Opposite 24 on C, find 568 on D. of CF Placing the decimal point by a rough calculation

$$\frac{254 \times 65 \times 24}{155 \times 45}$$
 is roughly  $\frac{250 \times 60 \times 25}{150 \times 50} = 50$ .

Hence, the result is 56.8,

Find the value of

Problem 154. 
$$\frac{3.26 \times .0235}{4.22}$$
.

Problem 158.  $.65 \times 24 \times 7.5 \times 9.5$ 

155. 
$$\frac{6.75 \times 1.35}{14.4}$$
.

159. 
$$\frac{6.45}{4.55 \times .0276}$$

156. 
$$26.4 \times 4.8 \times 7.12$$
.

160. 
$$\frac{1}{2.66 \times .75 \times 1.42}$$

167. 
$$6.2 \times 28 \times .35 \times 5.4$$
.

161. 
$$\frac{3}{2.54 \times 7.45}$$

Problem 162. 
$$\frac{2.14 \times 4.6 \times .39}{24.3 \times .06 \times .575}$$

163. 
$$\frac{5.8 \times 4.5 \times 8.7 \times 132}{7.3 \times 6.2 \times 28 \times 14}$$

164. 
$$\sqrt{\frac{2.63 \times 82.5}{2450}}$$

165. 
$$\sqrt{\frac{48.6 \times 22.4}{56.5 \times 245}}$$

166. 
$$\sqrt{\frac{22.5 \times 12.2 \times 126 \times 405}{2760 \times 715 \times 6.16}}$$

# MISCELLANEOUS CALCULATIONS

Example: Find the value of  $\frac{2.45 \times (76.5)^2 \times 625}{.55 \times .087}$ 

Method I. Use scales A and B, but use C for 76.5.

At 245 on A set 55 on B.

Indicator to 765 on C.

Set 87 on B to the indicator.

Indicator to 625 on B.

Opposite the indicator on A, find 187.

A rough calculation shows:

$$\frac{2 \times 70 \times 80 \times 600}{.5 \times .1} = \frac{200 \times 70 \times 80 \times 600}{5 \times 1} = 134000000.$$

The result is 187,000,000.

42 2

2.64

6

Method II. Write the example:

$$\frac{2.45 \times 76.5 \times 76.5 \times 625}{.55 \times .087 \times 1}$$

Method III. Find  $(76.5)^2$  as a separate problem, then work the example on  $\hat{C}$  and D.

Example: Find the value of  $\frac{135 \times \sqrt{475 \times 430}}{26 \times 250 \times 638}$ 

Use C and D, but use B for 475.

At 135 on D, set 26 on C.

Indicator to 4.75 on B (left half of slide, because the decimal point must be moved an even number of places).

Set 250 to the indicator.

Indicator to 430 on C.

Set 638 to the indicator.

On D, opposite the right-hand index, find 305.

Roughly calculating:

$$\frac{100 \times 20 \times 400}{25 \times 250 \times 600} = \frac{16}{75} = \text{about } \frac{1}{5}, \text{ or } .2$$

The result, then, is .305.

Example: Find the value of

$$\frac{\sqrt{260}\times\sqrt{3.80}}{\sqrt{1310}}.$$

Use A and B, but read the result on D.

At 2.6 on A set 13.1 on B (moving the decimal point an even number of places).

If we try to move the indicator to 3.8 on B, 3.8 projects beyond the end of the rule. Hence, move the indicator to the right index of the slide, then set the left index to the indicator. This operation divides by 100, but does not change the significant figures of the result.

Now move the indicator to 3.8 on B.

On D, opposite the indicator, read 869.

Roughly calculating:

$$\sqrt{\frac{300\times3}{1600}}=\frac{3}{4}=.75$$

Hence the result is .869.

Problem 167. 
$$\frac{13.5 \times (14)^2}{82}$$
 $A : To 135 : Find x$ 
 $B : Set 82 : C : Over 14$ 
 $D : C : Under 2$ 
 $C : Set 1 : D : To 135 : Find x$ 

Settings:

169.	42.3	A:	1	:	
105.	$\sqrt{6720}$	B:	Set 67	2	•
	€ 1000 date (100 date (10	C:			Under 10
		$\begin{array}{c} C : \\ \hline D : \\ A : \\ \hline B : \\ \hline C : \\ \hline D : \\ \hline B : \\ \hline C : \\ \hline D : \\ \end{array}$	To 42.3		Find x
170.	5.2	A:	To 5.2	:	Find $x$
110.	$(3.4)^2$	$B_{\widetilde{a}}$ :			Over 1
		$\underline{c}$ :	Set 3.4	<u>:</u>	
	(100) 150	D		:	T2' 1
171,	$(16.2)^2 \times 45.2$	<u>A</u> :		_:	Find x
	$(2.7)^2$	$\tilde{E}$ :	0-4-00	:	Over 452
		<u>c</u>	Set 27		
			To 162	•	
172	$\left\{ \frac{.0347}{.0058} \right\}^2$	A:		:	Find $x$
. ,	(.0058)	C:		:	Over 100
		D:	At 34'	7:	
173.	$2.31 \times (48.5)^2 \times 413$				
	$.45 \times .087$				
	$175 \times \sqrt{285} \times \sqrt{17} \times 410$				
174.	$28 \times 228 \times 634$				
	$\sqrt{8.32}  imes \sqrt{56.5}$				
175.					
	$\sqrt{2830}$				
176.	2.6				
	$(7.4)^3$				
177.	$\left\{ \frac{.0325}{.0075} \right\}^{3}$				
	(.0075)				
170	$^{3} \overline{420 imes1.65}$				

# CHAPTER IV

# PLANE TRIGONOMETRY

## SINES

The state of the s
* majoritaris in the second of
2 State of the control of the contro
The territory of the state of t
P. Tarantana Tarantana Baratan
mind between the beaution of the beaution of the beautiful and should be a second of the beautiful and

Fig. 28.

The scale marked S is a scale of sines. Angles are given on scale S, opposite their sines on scale B, and hence on scale A when the indexes of A and B coincide.

Example: Find sine 20°.

Opposite 20 on scale S is found its sine on scale B. This reads 342. To place the decimal point: a number read on the right half of scales A or B has the first significant figure in the first decimal place, except sine 90, which is 1; a number read on the left half of scales A or B has the first significant figure in the second decimal place.

Hence sine  $20^{\circ} = .3420$ .

Example: Find sine 2°.

The significant figures are 349.

The reading is on the left of scales A and B, hence the result is .0349.

# COSINES

Since the cosine of an angle is equal to the sine of the complement of the angle, the cosine may be found on the slide rule.

Example: Find cos 30°.

 $\cos 30^{\circ} = \sin (90^{\circ} - 30^{\circ}).$ 

 $= \sin 60^{\circ}$ . = .866.

Example: Find sin  $5^{\circ} 40' \times 35$ .

A : To 35

: Find 3.46

S: Set Right Index: Over 5° 40'

# Explanation

Log 35 is added to log sin 5° 40', the sum being counted on scale A.

Example: Find  $\frac{35}{\sin 5^{\circ} 40^{\circ}}$ 

A : To 35 S : Set 5° 40'

: Find 354.

To place the decimal point, note that  $\sin 5^{\circ} 40'$  is a trifle less than .1. This can be done just before setting down the answer by glancing at the value of the sine given under the indicator on the B scale. Hence, dividing 35 by .1, we have 350 for the rough calculation.

From  $\log 35$  we have subtracted  $\log \sin 5^{\circ} 40'$ , the difference being counted on scale A.

# EXERCISE

Problem	179.	Find	the	sine of	90°.	Problem	184.	Find	the	sine of	15° 20	٠.
	180.	"	66	46	45°.		185.	**	44		1° 30	۲.
	181.	14	46	44	30°.		186.	"	"	44	8° 30	1.
	182.	66	44	44	3°.		187.	"	"	46	2° 15	١.
	183.	16	"	71	40'.		188.	"	66	46	21° 30	١.

Problem	189.	Find	the	cosine	of 80°.	Problem	194.	Find	theco	sine o	of 75°	30'.
	190.	**	46	"	65°.		195.	46	"	44	54°	10'.
	191.	- 66	"	34	42°.		196.	44	"	66	$20^{\circ}$	30'.

199. Sin  $25^{\circ} \times 45$ .

**200.** Cos  $56^{\circ} \times 27$ .

**201.** 
$$\frac{18}{\sin 12^{\circ} 30'}$$

**Problem 203.**  $A = 32^{\circ}$ . (Fig. 29). c = 65

Find a.

Problem 204.  $A = 70^{\circ} 30'$ . a = 15.4. Find c.

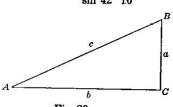


Fig. 29.

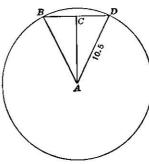


Fig. 30.

206. Holes A and C are to be drilled on the milling machine. After drilling C, in order to drill A, how much movement of the table will there be in each direction?

The table moves from C to B, then from B to A.

 $BC = 5 \times \cos 20^{\circ}$ .  $BA = 5 \times \sin 20^{\circ}$ . Problem 205. A disk is 21 inches in diameter. Find the distance necessary to set a pair of dividers in order to space off a,) 7 sides; b,) 8 sides; c,) 10 sides; d,) 13 sides.

The angle  $DAB = \frac{1}{7}$  of  $360^{\circ} = 51^{\circ} 26'$  (to the nearest minute).

The angle  $DAC = \frac{1}{2}$  of 51° 26′ = 25° 43′.

 $\frac{C}{A}\frac{D}{D}$  = sine angle DAC.

 $CD = AD \times \text{sine}$  angle DAC.  $BD = 2 \times CD = 2 \times AD \times \text{sine}$  angle DAC = d sine angle DAC where d = diameterof circle.

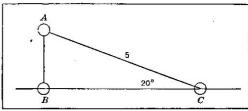


Fig. 31.

#### **TANGENTS**

* Linn	artinatification distribution	4 14 14 14 14 14 14 1	erialitatikaadaadaadaa	of the first of the first of the	danka ara da antasa da antagida.	Trianguist and the second
A tunion	make a local and a state of a to be built	de la companya de la	retraction with take the rest	andre bekerkelenings och i 14 felste	International production in the	ulimini anim Batanbatan
8			<del>a in train</del> material in ing	Andrea Landers and Control of the State of t	Martine Interestable	rafeer of complexity of
7 10.10	planta and a salar and a salar	والمسالية والموارية والمسالة والمسالة	New of the State of the Assessment	e techni oladi oladi oladi oladi oladi oladi e	n daes betalan berelanden den des Antonio	and the balance of
CT HHIAM	<del>Patriciphical International Control of the Control</del>	<del>ŢŢij</del>	i tali talahin bahahahah	And in the latter of the latter beinging	The bearing of the property of	क्रिक्टिक्कोक्शिक्कोक्शिक्कोक्का <u> </u>
1 1	I see the see the see	Creation designation	Contract to the contract of th	The state of the s		Called Andreas P

Fig. 32.

With the slide in position for reading sines, scale T gives readings for angles whose tangents are found opposite on scale D. Tangents may also be read directly on scale C, which eliminates the necessity of setting the indexes of the slide to the indexes of the scale.

The first significant figure comes in the first decimal place for all values

found on the rule.

Example: Find tan 30°.

Method I. Opposite 30 on scale T, find 577 on D.

Pointing off, we have  $\tan 30^{\circ} = .5770$ , which is correct to three significant figures, the result correct to four figures being .5774.

Method II. Set  $30^{\circ}$  on the T scale to 1 on D; and on C, opposite the indicator, read 577.

**Example:** Find the value of  $\tan 18^{\circ} 30' \times 175$ .

Find tan 18° 30' by method II.

Above 175 on D, find 586 on C. Or set left index of slide to 175 on D.

Opposite  $18^{\circ}$  30' on T read 586 on D.

Since tan  $18^{\circ} 30'$  is .334, the product must be roughly 1/3 of 175, making the result 58.6.

The scale gives tangents only as far as 45°.

For larger angles, use the formula:

$$\tan A = \frac{1}{\tan (90^\circ - A)}$$

Example: Find the tan of 75°.

$$\tan 75^{\circ} = \frac{1}{\tan (90^{\circ} - 75^{\circ})}$$

$$= \frac{1}{\tan 15^{\circ}}$$

Opposite the right index on scale D, set 15° on scale T. Opposite the left index on scale T, read 373 on scale D.

To place the decimal point, make a rough calculation, remembering that tan 45° = 1.

$$\frac{1}{\tan 15^{\circ}} = \frac{1}{\frac{1}{2}} = 3.$$

Hence the result is 3.73.

Owing to the presence of the CI scale we may also obtain the answer directly by setting the indicator at  $90^{\circ} - A$  and reading the tangent directly on the CI scale. This simplifies the operation, but is applicable only to angles less than

84°. For angles from 84° to 90°, the formula  $A = \frac{1}{\tan (90^{\circ} - A)}$  must be used. Tan  $(90^{\circ} - A)$  can be obtained by finding sine  $(90^{\circ} - A)$  as explained on page 47.

Example: Find the value of 565 ÷ tan 65°.

$$565 \div \tan 65^{\circ} = 565 \div \frac{1}{\tan 25^{\circ}}$$
$$= 565 \times \tan 25^{\circ}.$$

Find tan 25° by Method II. Opposite 565 on D find 263 on C. Or, set right index of slide to 565 on D. Opposite 25 on T find 263 on D. Example: Find the value of

512 ÷ tan 22° 30′.

Method I. To 512 on D, set 22° 30' on T.

Turn the rule over and opposite the index of C, find 1236 on D.

By a rough calculation, remembering that  $\tan 45^{\circ} = 1$ , we place the decimal point, making the result 1236.

Method II. Set  $22^{\circ} 30'$  on T to 1 on D.

Under 512 on C, find 1236 on D.

Method III. Set 22° 30' on T to 10 on D.

Above 512 on CF, find 1236 on DF.

The tangent of an angle less than  $5^{\circ}$  43' cannot be obtained directly from the ordinary 10 in. rule, but the sine may be used in place of the tangent, since the sine and the tangent of any of these angles are identical to three significant figures.

 $\tan 1^{\circ} 30' = \sin 1^{\circ} 30' = .0262.$ 

# COTANGENTS

The cotangents of angles from  $6^{\circ}$  to  $45^{\circ}$  may be read upon the CI scale In every case the first significant figure is a whole number.

Cotangents for angles greater than 45° may be found as follows:

Cot 
$$A = \tan (90^{\circ} - A) = \frac{1}{\tan A}$$

Example: Find cot 65°.

Cot 
$$65^{\circ}$$
 = tan  $(90^{\circ} - 65^{\circ})$ .  
= tan  $25^{\circ}$ .  
= .466.

Example: Find cot 18°.

$$Cot 18^{\circ} = \frac{1}{\tan 18^{\circ}}$$

# SECANT AND COSECANT.

The secant and cosecant may be found by the formulas:

$$\sec A = \frac{1}{\cos A}.$$

$$\csc A = \frac{1}{\sin A}.$$

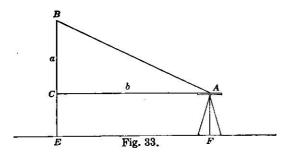
Problem 207. Find tangent of 25°. Problem 213. Find tangent of 75° 10'. 208. " " 14° 30'. 214. " " 20° 10'. " 35° 30'. 215. " " 15° 5'. 209. " " 6° 25'. 210. " " 26° 20'. 216. " 44 " 1° 45'. " 18° 30'. 217. 44 " 42° 20' 212. " " 55° 20'.

Problem 219. Tan 15° × 18.

Problem 220. Tan 65° 30′ 
$$\times$$
 13.2 =  $\frac{13.2}{\tan 24° 30′}$ 

Problem 221. 
$$\frac{5.62}{\tan 10^{\circ}}$$

Problem 222. 
$$\frac{8.5}{\tan 70^{\circ} 20'} = 8.5 \times \tan 19^{\circ} 40'$$
.



**Example:** To find BE, the height of a building, a transit is set up at A, a level line AC is sighted on a rod held at E.

CE is found to be 5.2 ft.

EF, which is equal to CA, is measured and found to be 138 ft. The angle CAB is taken by the transit and found to be 28° 30′.

Find BE, the height of the building.

$$BE = BC + CE,$$

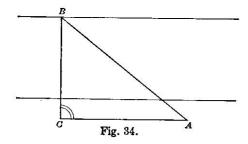
$$BC = CA \times \tan A.$$

$$BE = CA \times \tan A + CE.$$

$$= 138 \times \tan 28^{\circ} 30' + 5.2.$$

$$= 74.9 + 5.2.$$

$$= 80.1 \text{ ft.}$$



Example: To find CB, the width of a river.

A transit is set up at C and a right angle, BCA is laid off.

CA is measured and found to be 235 ft.

Then the transit is set up at A and the angle A found to be 75° 30′.

Find CB, the width of the river.

CB = 
$$CA \times \tan A$$
.  
= 235 ×  $\tan 75^{\circ}$  30'.  
=  $\frac{235}{\tan 14^{\circ} 30'}$ .  
= 909 ft.

# SINES AND TANGENTS OF SMALL ANGLES

Gauge points are placed on the sine scale for reading sines of angles smaller than those given on the regular scale. Near the 1° 10' division is the "second" gauge point and near the 2° division is the minute" gauge point. By placing one of these gauge points opposite any number on the A scale, the corresponding sine of that number of minutes or seconds is read over the index of the sine scale on A. Or place the gauge point opposite the left index. Then for any value on scale B the corresponding sine may be read on scale A for angles from 4' to 100' or from 3 " to 100", depending upon which gauge point is used. By placing the gauge point opposite the right index, sines for angles as small as 1" may be read. In order to point off, it should be remembered that sine 1" is about .000005 (5 zeros, 5), and sine 1' is about .0003 (3 zeros, 3).

The sines and tangents of small angles being practically identical, these gauge points, as well as the portion of the sine scale below  $5^\circ$  43', may also be

used for the tangents.

The tangents of angles greater than 89° 26' are found as follows: Determine  $90^{\circ}$  — A.

Set gauge-point to  $90^{\circ}$  — A on A.

Opposite right index of A read the tangent of  $(90^{\circ}$  — A) on B.

Opposite right index of A read the tangent of  $(90^{\circ} - A)$  on B. This is true because  $\tan (90^{\circ} - A)$  is the reciprocal of  $\tan A$ .

**Example:** Find sine 10". Opposite 10 on scale A set the gauge points for seconds. Opposite the left index find 485 on A. Since sine 1" = .000005,

sine 10" is roughly  $10 \times .000005$  or .00005. Hence sine 10" = .0000485.

Hence sine  $10^{\circ} = .0000485$ . Example: Find sine 12'.

Opposite 12 on scale A set the gauge point for minutes.

Opposite the left index find 349 on A. Since sine 1' = .0003,

Sine 12' is roughly 12 × .0003 = .0036.

Making 240 look or near as possible like .0036

Making 349 look as near as possible like .0036, sine 12' = .00349.

Example: Find tan 89° 45'.

 $90^{\circ} - 89^{\circ} 45' = 15'$ . Set minute gauge point to 15 on A.

Opposite right index of A read 229 on B. The tangent of 89° 45' is actually 229.18.

Example: Find  $\tan 89^{\circ} 45' 45''$ .  $90^{\circ} - 89^{\circ} 45' 45'' = 14' 15'' = 855''$ 

Set "second" gauge point to 855 on A. Opposite right index of A read 241 on B. The tangent of 89° 45′ 45″ is actually 241.46+,

Another method of finding sines and tangents of very small angles depends upon the fact that, for small angles the sine or the tangent varies directly as the angle.

Example: Find tan 15'.

Tan 15' = 
$$\sin 15'$$
,  
=  $\frac{1}{10} \sin 150'$ .  
=  $\frac{1}{10} \sin 2^{\circ} 30'$ .  
=  $\frac{1}{10}$ .0436 by the slide rule.  
= .00436.

# LOGARITHMS

The L scale is a scale of equal parts by which the logarithm of a number may be found.

Example: Find log 50.

Under 5 on scale D, find 699 on scale L.

This 699 is the mantissa. The characteristic is found by the usual rule, taking one less than the number of figures at the left of the decimal point. Since 50 has two such figures, its characteristic is 1.

Hence, log 50 is 1.699.

Example: Find  $(2.36)^5 = x$ .

$$Log x = 5 \times log 2.36.$$
  
= 5 \times .373.  
= 1.865.

Opposite 865 on the log scale find 732 on D.

$$x = 73.2.$$

Example: Find  $\sqrt[5]{187} = x$ .

Log 
$$187 = 2.272$$
.  
Log  $\sqrt[5]{187} = \frac{1}{5}$  of 2.272 = .454.

Problem 223. Find the logarithm of 1.34.

228. Find the value of  $(3.2)^5$ to three significant figures.

229. " " " 
$$(425)^4$$
. 230. " " "  $\sqrt[3]{3.46}$ - 231. " " "  $\sqrt[5]{286}$ .

Example:  $x = (2.7)^{1.41}$ 

$$\log x = 1.41 \times \log 2.7 \\ = 1.41 \times 0.431$$

(Log 2.7 found on slide rule as in first example).

$$=0.608$$
 (Multiply, using scales  $C$  and  $D$ ).

x = 4.05

Example:  $x = (41.5)^{0.23}$ 

$$\log x = 0.23 \times \log 41.5$$

 $= 0.23 \times 1.618$ 

(Find mantissa of  $\log 41.5 = .618$ ). Then prefix characteristic of 1, making 1.618.)

= 
$$0.372$$
 (Multiply, using scales  $C$  and  $D$ ).

x = 2.36 $\log x = \log 51.3$ 

x = 2.56

Example:  $x = 1^{2} 51.3$ .

$$= \frac{1.710}{4.2}$$
=\frac{1.710}{4.2} \quad \text{(Finding log 51.3 = 1.710).}
= .0407 \quad \text{(Divide; using scales \$C\$ and \$D\$).}

# To Change Radians to Degrees or Degrees to Radians

		π	Radians .	
		180	Degrees	
A	Opposite π	Opposite	Radians	Read Radians
B	Set 180	Read I	Degrees — or	Opposite Degrees

# CHAPTER V

# SOLUTION OF TRIANGLES

By the Slide Rule a right triangle or an oblique triangle may be solved in a few seconds. On the 10" Slide Rule a side of a triangle may be read to three significant figures, and the angles to within a few minutes. For many kinds of applied work this degree of accuracy is sufficient.

Where greater accuracy is required, as in surveying calculations, the work should be done by logarithms, and then checked by the slide rule. This check will show any gross error and will locate the error. For classes in Trigonometry it is recommended that the student proceed as follows:

- a. Solve the triangle by logarithms.
- b. Check by solving on the Slide Rule.
- c. If the Slide Rule shows that there is an error, find the error and correct it.
- d. If no error appears and it is desired to check to a greater degree of accuracy, apply the usual trigonometric check.

The use of the Slide Rule saves time and locates the error in a particular part of the work.

NOTE: In the following pages on right and oblique triangles the author has drawn freely upon the admirable treatment of this subject in a chapter of the former Mannheim Manual by Professor J. M. Willard, of the State College of Pennsylvania.

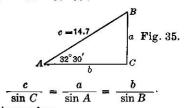
## RIGHT TRIANGLES

Example: Given an Acute Angle and the Hypotenuse.

Let 
$$A = 32^{\circ} 30'$$
 and  $c = 14.7$ .

Find B, a, and b.

Solution:  $B = 90^{\circ} - A = 57^{\circ} 30'$ .



Substituting the given values.

$$\frac{14.7}{\sin 90^{\circ}} = \frac{a}{\sin 32^{\circ} 30'} = \frac{b}{\sin 57^{\circ} 30'}$$

Setting the rule as in proportion, using right half of scale A,

$A \mid$	Opposite 14.7	Read $a = 790$	Read $b = 124$
S	Set 1 (sin 90°)	Opposite 32° 30'	Opposite 57° 30'

To place the decimal point, note that the sides will be in the same order of magnitude as their opposite angles.

$$C = 90^{\circ}$$
  $c = 14.7.$   
 $B = 57^{\circ} 30'$   $b = 12.4.$   
 $A = 32^{\circ} 30'$   $a = 7.88.$ 

Where the S scale is involved, care should be taken to set the number on the proper half of scale A. The following diagram will make this clear. The numbers on the scale are continuous.

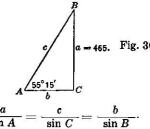
· Left End	Middle	Right End
.01	.1	1.
Scale A 1.	10.	100.
100.	1000.	10000.

Example: Given an Acute Angle and the Opposite Side.

Let  $A = 55^{\circ} 15'$  and a = 465.

Find B, b, and C.

Solution:  $B = 90^{\circ} - A = 90^{\circ} - 55^{\circ} 15' = 34^{\circ} 45'$ .



Using left half of scale A.

A	Opposite 465	Find $c = 566$	Find $b = 323$
S	Set 55° 15'	Opposite 1 (sin 90°)	Opposite 34° 45

Placing the decimal point,

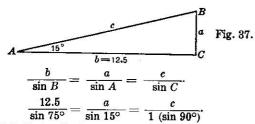
$$C = 90^{\circ}$$
  $c = 566.$   
 $A = 55^{\circ} 15'$   $a = 465.$   
 $B = 34^{\circ} 45'$   $b = 323.$ 

Example: Given an Acute Angle and the Adjacent Side.

Let  $A = 15^{\circ}$ , b = 12.5.

Find B, a, and c.

Solution:  $B = 90^{\circ} - A = 75^{\circ}$ .



Using the right half of scale A.

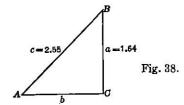
$A \mid$	Opposite 12.5	Find $a = 3.35$	Find $c = 12.9$
S	Set 75°	Opposite 15°	Opposite 90°

Placing the decimal point by arranging the angles and sides in order,

$$C = 90^{\circ}$$
  $c = 12.9.$   
 $B = 75^{\circ}$   $b = 12.5.$   
 $A = 15^{\circ}$   $a = 3.35.$ 

**Example:** Given the Hypotenuse and a Side. Let a = 1.64, c = 2.55

Find A, B and b.



Solution: 
$$-\frac{c}{\sin C} = \frac{a}{\sin A} = \frac{b}{\sin B}$$
.  
 $\frac{2.55}{1(\sin 90^{\circ})} = \frac{1.64}{\sin A} = \frac{b}{\sin B}$ .

B may be found after A is known.

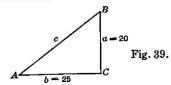
$$B = 90^{\circ} - 40^{\circ} = 50^{\circ}$$
.

To place the decimal point in b:

Since B is a little larger than A, b will be a little larger than a.

Hence b = 1.95.

Example: Given the Two Sides.



Case I. Where  $\tan A$  or  $\frac{a}{b}$  is less than 1.

Let a = 20 and b = 25.

Find A, B and c.

Solution: 
$$\frac{a}{b} = \frac{\tan A}{1 (\tan 45^{\circ})} \text{ or } \frac{b}{1} = \frac{a}{\tan A}$$

$$\frac{T}{D} = \frac{\text{Set } 1 (\tan 45^{\circ})}{\text{Opposite } 25} = \frac{F \text{ind } A = 38^{\circ} 40'}{\text{Opposite } 20}$$

Or  $\tan A = \frac{20}{25}$ 

$D \mid$	Opposite 25	Opposite right index
C	Set 20	
T		Ti' 1 4 900 401
		Find $A = 38^{\circ} 40'$

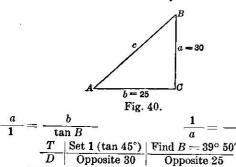
To find c, use the formula,  $\frac{a}{\sin A} = \frac{c}{\sin C}$ 

Case II. When  $\tan A$  or  $-\frac{a}{b}$  is greater than 1.

Let a = 30, b = 25.

Find A, B and c.

Solution: Find B first in order to avoid finding the tangent of an angle greater than  $45^{\circ}$  since the T scale reads only to  $45^{\circ}$ .



Or 
$$\tan B = \frac{25}{30}$$

$D \mid$	Opposite 30	Opposite right index
C	Set 25	
$\underline{T}$		
		Find B = $39^{\circ} 50'$

$$A = 90^{\circ} - 39^{\circ} 50' = 50^{\circ} 10'$$
.

Find c by the formula 
$$\frac{b}{\sin B} = \frac{c}{\sin C}$$

# OBLIQUE TRIANGLES

Example: Given Two Angles and a Side.

Let 
$$a = 22.5$$
  $A = 44^{\circ} 30'$   $B = 24^{\circ} 15'$ 

Find C, b and c.

Solution: 
$$C = 180^{\circ} - (44^{\circ} 30' + 24^{\circ} 15')$$
  
 $180^{\circ} - 68^{\circ} 45'$   
 $111^{\circ} 15'$ 

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C \text{ or } \sin (A+B)}$$
$$\frac{22.5}{\sin 44^{\circ} 30'} = \frac{b}{\sin 24^{\circ} 15'} = \frac{c}{\sin 111^{\circ} 15' (\sin 68^{\circ} 45')}$$

Using the right half of rule:

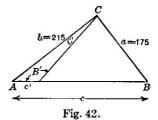
<u>A</u> _	Opposite 22.5	Find $b = 132$	Find $c = 299$
$\boldsymbol{S}$	Set 44° 30'	Opposite 24° 15'	Opposite 68° 45'

To place the decimal point, the sides will follow the same order of magnitude as their opposite angles.

$$C = 111^{\circ} 15'$$
  $c = 29.9.$   
 $A = 44^{\circ} 30'$   $a = 22.5.$   
 $B = 24^{\circ} 15'$   $b = 13.2.$ 

**Example:** Given Two Sides and the Angle Opposite One of these Sides. This example has two possible solutions, both of which are given below.

Let 
$$a = 175$$
.,  $b = 215$ .,  $A = 35^{\circ} 30'$   
Find B, C, and c, B' and c'



Solution: 
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
. Note: Sine  $C = \text{Sine } (A + B)$ .

Using left half of rule.

$$\begin{array}{c|c|c} \underline{A} & | \text{Opposite 175} & | \text{Opposite 215} & | & \text{Find } c = 298 \\ \hline Set 35^{\circ} 30' & | & \text{Find } B = 45^{\circ} 30' & | & \text{Opposite } (A+B) \text{ or } 81^{\circ} \\ \hline \\ B' = 180^{\circ} - 45^{\circ} 30' & (B), \\ & = 134^{\circ} 30', \\ A+B' = 35^{\circ} 30' + 134^{\circ} 30', \\ & = 170^{\circ}, \\ C' = 180^{\circ} - 170^{\circ}, \\ & = 10^{\circ}. \end{array}$$

Indicator to right index Find 
$$c' = 52.2$$

Left index to indicator Opposite  $C' = 10^{\circ}$ 

To place the decimal point, arrange angles and sides in order of magnitude. In triangle ABC,

$$C = 99^{\circ}$$
  $c = 298.$   $B = 45^{\circ} 30'$   $b = 215.$   $A = 35^{\circ} 30'$   $a = 175.$ 

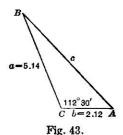
In triangle AB'C,

$$B'= 134^{\circ} 30'$$
  $b=215.$   
 $A= 35^{\circ} 30'$   $a=175.$   
 $C'= 10^{\circ} 0'$   $c'=52.2.$ 

Example: Given Two Sides and the Included Angle. The fact that the tangent scale runs only to  $45^\circ$  makes two cases.

Case I. When  $\frac{C}{2}$  is greater than 45° whence  $\frac{1}{2}(A + B)$  is less than 45°.

**Example:** 
$$a = 5.14$$
,  $b = 2.12$ ,  $C = 112^{\circ} 30'$ . Find  $A, B$  and  $c$ .



Solution:

$$a = 5.14$$
.

$$b = 2.12$$
.

$$a+b=7.26$$
.

$$a-b=3.02$$
.

$$A + B = 67^{\circ} 30'$$
.

$$\frac{1}{2}(A+B) = 33^{\circ} 45'$$
.

$$\frac{\frac{1}{2}(A-B)=15^{\circ} 32'}{A} = 49^{\circ} 17'.$$

$$A = 49^{\circ} 17'.$$
 $B = 18^{\circ} 13'.$ 

Use the formula,

$$\frac{\tan \frac{1}{2} (A + B)}{a + b} = \frac{\tan \frac{1}{2} (A - B)}{a - b}.$$

$$\frac{T}{D} | \frac{\text{Set } \frac{1}{2} (A+B)}{\text{Opposite } (a+b)} | \frac{1}{2} (A-B)$$

$$\frac{T}{D} \begin{vmatrix} \text{Set } 33^{\circ} 45' \\ \text{Opposite } 7.26 \end{vmatrix}$$
 Find  $\frac{1}{2}$   $(A-B) = 15^{\circ} 32'$ .

c is found by the usual sine formula:

$$\frac{a}{\sin A} = \frac{c}{\sin C}$$

$$\frac{5.14}{\sin 49^{\circ} 17'} = \frac{c}{\sin 112^{\circ} 30' \text{ or } \sin 67^{\circ} 30'}$$

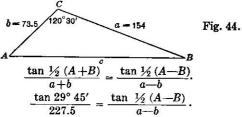
$$\frac{A}{S} = \frac{Opposite 5.14 \text{ (Left half of scale A)}}{\text{Set } 49^{\circ} 17'} = \frac{Find \ c = 6.27}{Opposite 67^{\circ} 30'}$$

$$\frac{c}{\sin C} = \frac{b}{\sin B}.$$

$$\frac{A}{S} = \frac{Opposite 6.27 \text{ (Left half of scale A)}}{\text{Set } 67^{\circ} 30'} = \frac{Find \ 2.12}{Opposite 18^{\circ} 1}$$

Opposite 18° 13' NOTE:- In the mathematics classroom this check formula may be used after the student has solved the triangle by logarithms.

Example: a = 154, b = 73.5,  $C = 120^{\circ} 30'$ .



Solution:

Set 29° 45' | Indicator to right index | Find  $\frac{1}{2}$  (A-B) = 11° 26' D Opposite 227.5 Left index to indicator Opposite 80.5  $\frac{1}{2}(A+B)=29^{\circ}45'$ .

 $\frac{1}{2}(A-B)=11^{\circ}26'$ .

 $A = 41^{\circ} 11'$ .

 $B = 18^{\circ} 19'$ .

By the method of the preceding example, c is found to be 202.

When  $\frac{C}{2}$  is less than 45°, whence  $\frac{1}{2}(A+B)$  is greater than 45°.

**Example:** a = 75.5, b = 42.5,  $C = 65^{\circ} 30'$ .

$$a+b=118$$
,  $a-b=33$ .

$$\frac{1}{2}(A+B) = 57^{\circ} 15'$$
.

$$\frac{\tan \frac{1}{2}(A+B)}{a+b} = \frac{\tan \frac{1}{2}(A-B)}{a-b}$$

$$\frac{\tan 57^{\circ} 15'}{118} = \frac{\tan \frac{1}{2}(A-B)}{33}$$

Since tan 57° 15' is not on the rule, we substitute for it

$$\frac{1}{\tan (90^{\circ}-57^{\circ} 15')} = \frac{1}{\tan 32^{\circ} 45'}$$

The formula now reads:

$$\frac{1}{118 \times \tan 32^{\circ} 45'} = \frac{\tan \frac{1}{2} (A-B)}{33}.$$

T | Set 1 (Left index) | Indicator to 32° 45′ | Find  $\frac{1}{2}$  (A-B) = 23° 30′ D Opposite 118 Right index to indicator

 $\frac{1}{2}(A+B) = 57^{\circ} 15'$ .

 $\frac{1}{2}(A-B) = 23^{\circ}30'$ .

 $A = 80^{\circ} 45'$ .

B = 33 45'.

Find c by the usual method.

Check by the sine formula.

Example: b = 83.4, a = 78,  $C = 72^{\circ} 15'$ .

b+a=161.4b-a = 5.4

 $\frac{1}{2}(B+A) = 53^{\circ} 53'$ .

T |Set 1 (Right index)| Indicator to 36° 7' Find 24° 38' Opposite 161 Left index to indicator Opposite 5.4

 $\frac{1}{2}(B-A) = 24^{\circ} 38'$ .

Testing these results by the formula:

 $B = 78^{\circ} 31'$ .  $A = 29^{\circ} 15'$ .

$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

it will be found that the angles are incorrect. This results from the fact that the slide rule gives the significant figures of the tangent, but does not fix the decimal point. In this example, there are three values for  $\frac{1}{2}$  (B-A) between 2° and 88°, corresponding to the natural tangent whose significant figures are

- 1.  $tan^{-1}.0459 = 2^{\circ} 38'$
- 2.  $tan^{-1}.459 = 24^{\circ} 38'$
- 3.  $tan^{-1} 4.59 = 77^{\circ} 43'$

Other values may be found less than 2° or between 88° and 90°, but these will seldom be required.

Hence, in the solution of any problem in this case, it is necessary to test the results by the check formula.

An inspection shows that b is slightly larger than a. Hence B will be only slightly larger than A. This would be possible if  $\frac{1}{2}(B-A)$  were smaller than 24° 38', which we obtained on the rule.

Find tan 24° 38', which is .459.

Find tan-1 .0459.

In order to secure this small angle, we use the sine scale, since the sine of an angle less than 5° 43' is practically equal to the tangent.

Opposite .0459 on the left half of scale A, find 2° 38' on S.

$$\frac{1}{2}(B+A) = 53^{\circ} 53'$$

$$\frac{1}{2}(B-A) = 2^{\circ} 37'$$

Using the check formula, 
$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

$$B = 56^{\circ} 30'$$
.

$$A = 51^{\circ} 15'$$
.

these results will be found to be correct.

Suppose it is desired to obtain the next larger angle than 24° 38'.

$$\tan 24^{\circ} 38' = .459.$$

The next larger angle with the same significant figures for the tangent would be:  $\tan x = 4.59$ .

Since this angle is evidently greater than 45°, we may write:

$$\tan (90^{\circ}-x) = \frac{1}{\tan x} = \frac{1}{4.59}$$

Solving by the slide rule

T |Set 1 (tan 45°) |Find 12° 17'  
D | Opposite 4.59 |Opposite 1  

$$90^{\circ}$$
— $x = 12^{\circ}$  17'.  
 $x = 77^{\circ}$  43'.

Or, opposite 4.59 on the CI scale read 12° 17', which is equal to  $90^{\circ}-x$ .

Example: 
$$a = 10$$
,  $b = 90$ ,  $C = 65^{\circ}$ .  
 $b + a = 100$ .  $b - a = 80$ .

$$b+a=100.$$

$$\frac{1}{2}(B+A) = 57^{\circ} 30'$$
.  
 $\frac{1}{2}(B-A) = 7^{\circ} 10'$ . by the first trial on the rule.

$$B = 64^{\circ} 40'$$
.

$$A = 50^{\circ} 20'$$
.

These results do not check.

Since b is nine times a, B must be considerably larger than A.

Using the method above,

$$\tan 7^{\circ} 10' = .126.$$
  
 $\tan x = 1.26.$ 

$$\tan (90^{\circ}-x) = \frac{1}{1.26}$$

Or read 38° 32' opposite 1.26 on the CI scale.

$$90^{\circ}-x = 38^{\circ} 32'$$
.

$$x = 51^{\circ} 28'$$
.

$$\frac{1}{2}(B+A) = 57^{\circ} 30'$$
.

$$\frac{1}{2}(B-A) = 51^{\circ} 28'$$
.

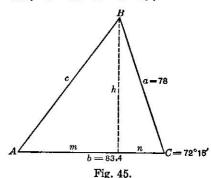
$$B = 108^{\circ} 58'$$
.

$$A = 6^{\circ} 2'$$
.

These results check by the formula 
$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

# ANOTHER METHOD.

Example: b = 83.4, a = 78.  $C = 72^{\circ} 15'$ .



$$h = a \sin C = 74.3$$

$$n = a \cos C = a \sin (90^{\circ} - C) = 23.8$$

$$m = b - n = 59.6$$

$$90^{\circ}-A = \tan^{-1} \frac{m}{h} = 90^{\circ}-38^{\circ} 45'$$

$$A = 51^{\circ} 15'$$

$$B = 180^{\circ} - (A + C) = 56^{\circ} 30'$$

$$C = \frac{h}{\sin A} = 95.3$$

Check, 
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Example: Given three sides.

Method I. Let 
$$a = 32.0$$
.

0. 
$$b = 26.5$$
,  
Find A, B, and C.

$$a = 32.0.$$

$$b = 26.5$$
.

$$c = 14.7$$
.

$$2s = 73.2$$
.

$$s = 36.6$$
.

$$s-a = 4.6$$
.

$$s-a = 4.0.$$
  
 $s-b = 10.1.$ 

$$s-c = 21.9$$
.

$$=\sqrt{rac{10.1 imes21.9}{26.5 imes14.7}}\cdot$$

c = 14.7.

$$= 0.754$$
. By the slide rule.

 $\sin \frac{1}{2} A = \sqrt{\frac{(s-b)(s-c)}{bc}}.$ 

Hence  $\frac{1}{2}A = 49^{\circ}$ (Using scales A and S).  $A = 98^{\circ}$ 

Find B and C by the formula:

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{32}{\sin 98^{\circ}(=\sin 82^{\circ})} = \frac{26.5}{\sin B} = \frac{14.7}{\sin C}$$

Method II. 
$$\cos C = \frac{a^a + b^a - c^a}{2ab}$$
.

or Sin (90° — C) = 
$$\frac{1024. + 702. - 216.}{1696.} = \frac{1510}{1696}$$

Sin 
$$(90^{\circ} - C) = .890$$
  
 $90^{\circ} - C = 63^{\circ}$  (to the nearest degree)  
 $C = 27^{\circ}$ 

Find B from the formula 
$$\frac{c}{\sin C} = \frac{b}{\sin B}$$

and A from the formula 
$$\frac{c}{\sin C} = \frac{a}{\sin A}$$
.

Check:  $A + B + C = 180^{\circ}$ .

Example: Given the three sides:-

$$a = 20, b = 18,$$

$$c = 1$$

c = 15.

Find the angles A, B and C.

An easy indirect solution suited to the slide rule is as follows:

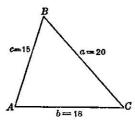


Fig. 44.

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}.$$

$$A + B + C = 180^{\circ}$$

By inspection a is the longest side, hence angle A is the greatest angle and is greater than 60°.

To 20 on scale A set trial value of A on scale S; opposite sides b and c on A read corresponding angles on S. Only a few trials are necessary.

# CHAPTER VI

# TYPICAL EXAMPLES RELATING TO VARIOUS OCCUPATIONS

# SECRETARIAL WORK

A secretary in checking a traveling man's expense account for one week found the following items:

Railroad fares	\$27.50
Hotel bills	56.00
Total	83.50

Find what per cent of the total expense was used in hotel bills.

Solution:  $56 \div 83.50 = 67$  per cent.

Opposite 56 on D set 835 on C.

Opposite the right index of C, find 67 on D.

## EXCAVATING

What will be the cost of excavating rock for a cellar measuring 43 ft × 28 ft. to an average depth of 6.5 ft. at \$2.50 per cubic yard?

$$x = \frac{43 \times 28 \times 6.5 \times 2.5}{27}$$

- 1. To 43 on D set 27 on C.
- 2. Indicator to 28 on C.
- 3. 65 on CI to indicator.
- 4. Opposite 25 on C read 725 on D.

Roughly calculating for the decimal point:-

x = 800.

Hence, the result is \$725; which is correct to the nearest dollar.

## PER CENT OF PROFIT

A merchant purchased a bill of goods for \$318 and sold the same for \$360. Find the per cent of profit reckoned,

- a. On the cost.
- b. On the selling price.

Solution: Profit = \$360 - \$318 = \$42.

Per cent of profit reckoned on the cost =  $\frac{42}{218}$  = 13.2 per cent.

Per cent of profit reckoned on the selling price =  $\frac{42}{360}$  = 11.7 per cent.

## DISCOUNT

Simple discount is set by reading the scales backwards, deducting from 100, thus, for a discount of 18%, set right hand (or middle) index at 82 (100 - 18 = 82) and the rule is set, so that opposite any number on C, the answer will be found on D, or opposite any number on CF, the answer will be found on DF. This is equivalent to multiplying by 82%.

For a combination of discounts, set by the use of the indicator, thus for

 $27\frac{1}{2} - 15 - 5\%$ , proceed as follows:

$\boldsymbol{c}$	Right Ind.	Ind. to 85 (100-15)	R to Ind.	Ind. to 95 (100-5)	R to Ind.	Opp. any amount
	To 72.5 (100-27 1/2)					Find answer

For frequently occurring discounts, a gauge mark should be made.

#### COMPOUND INTEREST

How many years will it take a sum of money to double itself if deposited in a savings bank paying 4 per cent interest, compounded semi-annually.

Using the formula  $A = P(1+r)^n$ , where A is the amount, P the principal, r the interest on \$1. for 6 months, and n the number of half years, if we take \$1. as P, we have:

$$2 = (1+.02).^{n}$$
  
and  $n = \frac{\log 2}{\log 1.02}$ .  
 $= \frac{.301}{.0086}$ . See page 45.  
 $= 35$  half years. See page 11.  
or  $17\frac{1}{2}$  years.

NOTE.—It is advisable to use a 20-inch rule for this problem. On the 10-inch rule the result can be found only very roughly.

# PHYSICS

In a photometer a 16 c. p. lamp is used as a standard. The following distance readings are obtained in testing a nitrogen filled lamp.

D <sub>8</sub>	$\mathbf{D}_{m{x}}$			
317 mm.	683 mm.	Ву	experiment	1
304 mm.	696 mm.	**	44	2
322 mm.	678 mm.	"	**	3
248 mm.	570 mm.	**	44	4

Using the following equation calculate the observed candle power of the unknown lamp.

$$\frac{D_s^2}{D_x^2} = \frac{\text{c. p. of standard}}{\text{c.p. of unknown}}$$
$$\frac{(317)^2}{(683)^2} = \frac{16}{x}.$$

To 683 on scale D set 317 on C.

Above 16 on B find x on A.

$$x = 74.4.$$

The operation of transferring from scales C and D to A and B squares the fraction  $\frac{317}{683}$ .

# CHEMISTRY

By weight 80 parts of sodium hydroxide combine with 98 parts of sulphuric acid. How many grams of sodium hydroxide will neutralize 50 grams of

sulphuric acid?

Solution: 
$$98 : 50 = 80 : x$$
.  
To 50 on  $D$  set  $98$  on  $C$ .

Under 80 on C find 40.8 on D.

## SPEEDS OF PULLEYS

The diameter of the driving pulley is 9 inches and its speed is 1,300 R. P.M. If the diameter of the driven pulley is 7 inches, what is its speed?

Solution: The diameter of the driving pulley, multiplied by its speed, is equal to the diameter of the driven pulley, multiplied by its speed.

$$7 \times S = 9 \times 1300.$$

$$S = \frac{9 \times 1300}{7}.$$

See page 13.

S = 1670 correct to three significant figures

# CUTTING SPEED

A certain grindstone will stand a surface or rim speed of 800 ft. per min. At how many R. P. M. can it run if its diameter is 57 in.?

Solution: The cutting speed is equal to the circumference of the stone in feet multiplied by the number of revolutions per minute.

or C = 
$$\frac{\pi \text{ d} \times \text{R. P. M.}}{12}$$
 where d is expressed in inches.  
Hence R. P. M. =  $\frac{12 \text{ C}}{\pi \text{ d}}$ .  
=  $\frac{12 \times 800}{3.1416 \times 57}$ .  
= 53. See page 34.

# GEARING

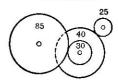


Fig. 45.

The gear with 85 teeth (Fig. 45) revolves 50 times per minute. Find the speed of the gear with 25 teeth.

Solution: The continued product of the R. P. M. of the first driver and the number of teeth in every driving gear is equal to the continued product of the R. P. M. of last driven gear and the number of teeth in every driven gear.

Hence, 
$$50 \times 85 \times 40 = 30 \times 25 \times S$$
.  

$$S = \frac{50 \times 85 \times 40}{30 \times 25}$$
. See page 33.  

$$S = 227$$
.

# LENGTH OF PATTERN

If window weights are  $1\frac{1}{2}$  inches in diameter, how long must we make the pattern for 8 lb. weights (1 cu. in. of cast iron weighs .26 lb.)?

Solution: The number of pounds in the window weight is equal to the volume of the cylindrical weight × .26 lb.

$$8 = \frac{\pi \times (1.5)^{3} \times L \times .26}{4}.$$
and  $L = \frac{4 \times 8}{\pi \times (1.5)^{3} \times .26}$ . See page 34.
$$= 17.4 \text{ inches, or } 17 \text{ and } 7/16 \text{ inches to the nearest16th.}$$

## COMPOSITION METAL MIXING

If bell metal is made of 25 parts of copper to 11 parts of tin in weight, find the weight of each metal in a bell weighing 1054 lbs.

Solution: The copper weighs 
$$\frac{25}{36}$$
 of 1054 = 732 lbs. See page 13.

The tin weighs 
$$\frac{11}{36}$$
 of 1054 = 322 lbs.

## SURVEYING

The slide rule is used in surveying to check gross errors in computation, to reduce stadia readings, and to solve triangles.

See page 47 for the solution of triangles by the slide rule.

Example: Find the latitude and departure of a course whose length is 525 ft. and bearing N 65° 30′ E.

Latitude = length of course 
$$\times$$
 cosine of bearing.  
=  $525 \times \cos 65^{\circ} 30'$ .  
=  $525 \times \sin 24^{\circ} 30'$ .  
=  $218$ .

Opposite the right index of A, set 24° 30′ on scale S.

Opposite 525 on A, find 218 on B.

The decimal point may be placed by inspection, since the sine and cosine are always less than one.

Departure = length of course 
$$\times$$
 sine of bearing.  
=  $525 \times \sin 65^{\circ} 30'$ .  
=  $478$ .

NOTE.- Keuffel and Esser Co. make a special rule for surveyors, known as the Surveyor's Duplex Slide Rule, which, has not only the A,B,CI,C and D scales on one face, but two full length stadia scales for computing horizontal distances and vertical heights. The other face is arranged for the determination of the meridian by direct solar observations, and carries the sine and cosine scales used in calculating latitudes and departures of the course. Hence, this rule reduces many complicated surveying calculations to mere mechanical operations.

For those who desire to calculate stadia reductions, and latitudes and departures, with a considerable degree of accuracy, the above mentioned company makes a complete Stadia slide rule.

# <del>-- 63 --</del>

# Rectangular Co-Ordinates

$$c = \sqrt{a^2 + b^2} = a \sqrt{1 + \frac{b^3}{a^2}}$$

$\underline{c}$	Set a				At a	Read $\frac{a}{c}$
D	At b				Read $\sqrt{a^2+b^2}$	At 1
В		At 1	Mentally add 1	Set 1		
A		$rac{\left(\frac{b}{a}\right)^2}$		$at 1 + \left(\frac{b}{a}\right)^{2}$		

or

C	Set b				At a	Read $\frac{a}{c}$
D	Ata				Read $\sqrt{a^2+b^2}$	At 1
$\overline{B}$		$\overline{\text{Read}\Big(\frac{b}{a}\Big)^2}$	add I to	Set 1		
A		At 1	$\frac{\mathbf{b}^{2}}{\mathbf{a}^{2}}$	$at 1 + \left(\frac{b}{a}\right)^{1}$		

or

C	Set b				Read $\sqrt{a^2+b^2}$	At 10
D	At a	Set Ind. at $\frac{a}{b}$			At a	Read $\frac{\mathbf{a}}{\mathbf{c}}$
В			$\overline{\operatorname{Read}\left(\frac{\mathrm{b}}{\mathrm{a}}\right)^2}$	$\frac{\text{Move}}{1+\left(\frac{\mathbf{b}}{\mathbf{a}}\right)^2}$		
$\boldsymbol{A}$			At 1	То 1		

# Example:

Find the diagonal of a rectangle with sides 61 and 111 feet in length.

Diagonal = 
$$\sqrt{(6\frac{1}{2})^2 + (11\frac{1}{2})^2} = 6\frac{1}{2}\sqrt{1 + \left(\frac{11\frac{1}{2}}{6\frac{1}{2}}\right)^2}$$

To  $11\frac{1}{2}$  on D set  $6\frac{1}{2}$  on C.

Opposite right index read 3.13 on A.

Adding 1 = 4.13.

Set right index of slide to 4.13 on A.

Opposite 6.5 on D read 13.21. Answer.

This solution required only two settings of the rule. Compare this with the solution required if the equation had remained in its original form. This would have required 3 settings and an addition on paper.

# CHAPTER VII

# METHODS OF WORKING OUT MECHANICAL AND OTHER FORMULAS

Diameters and Areas of Circles

 $A = .7854 D^2$ 

The B scale has .7854  $\left(\frac{\pi}{4}\right)$  marked by a long line on the left half.

A	R. Index	· - /		A	To 11	
В	Set .7854	Find Areas.		В	Set 6	Find Areas in square feet
C			or	C		
D		Above Diameters		D		Above Diameter in inches

# To Calculate Selling Prices of Goods, wi h percentage of profit on Cost Price

C	Set 100	Below cost price	
$\mathbf{D}$	To 100 plus percentage of profit	Find selling price	

# To Calculate Selling Prices of Goods, with percentages of profit on Selling Price

C	Set 100 less percentage of profit	Below cost price
D	To 100	Find selling price

Example: If goods cost 45 cents a yard, at what price must they be sold to realize 15 per cent profit on the selling price?

С	Set 85 (=100—15)	Below 45
D	To 100	Find 53—Answer

To find the Area of a Ring

 $\mathbf{A} = \frac{(\mathbf{D} + \mathbf{d}) \times (\mathbf{D} - \mathbf{d})}{\mathbf{d}}$ 

$\mathbf{D} \parallel$	To sum of the two diameters	Find area
$\overline{\mathbf{c}}$	Set 1.273	Under difference of the two diameters

# Compound Interest [Log A = Log P + n Log (1+r)]

Opposite 1 plus the rate of interest on D, find the corresponding number on the L scale and multiply it by the number of years.

Set the indicator to this product on the L scale.

Set index of C to the indicator.

Opposite the principal on C, read the amount for the given number of years at the given rate on D.

Example: Find the amount of \$150. at 5 per cent at the end of 10 years.

D	Set Ind. to 105			Read \$244.35 Ans.
L	Read .0212	Ind.to.2(.0212×10)		
$\overline{C}$			Left Index to Ind.	Opposite 150

#### Lever

C Set distance from fulcrum to power or weight transmitted		Below power or weight applied.	
D	To distance from fulcrum to power or weight applied	Find power or weight transmitted	

# Diameter of Pulleys or Teeth of Wheels (See page 61)

C	Set diameter or teeth of driving	Revolutions of driven
D	To diameter or teeth of driven	Revolutions of driving

# Diameter of two Wheels to work at given Velocities

C	Set distance between their centers	Find diameter
D	To half sum of their revolutions	Above revolutions of each
	Show at 1 of 70 at	$\sqrt{\overline{\mathrm{H}}}$

Strength of Teeth of Wheels  $P = \frac{\sqrt{H}}{0.6V}$ 

A	To H. P. to be transmitted			7
В		<u> </u>		1
C	Set gauge point 0.6	R to 1	Velocity in ft. per second to R	Under 1
D				Pitch in inches

Diameter and Pitch of Wheels

 $N = \frac{D \times \pi}{P}$ 

DF	To D	Find number of teeth
$\mathbf{CF}$	Set P	Opposite #

# Strength of Wrought Iron Shafting

$$D = \sqrt[3]{\frac{83 \, H}{N}}$$
 for crank shafts and prime movers

$$D = \sqrt[3]{\frac{65 \text{ H}}{N}} \text{ for ordinary shafting}$$

C	Set revolutions per minute	Ind. to Ind. H. P.	
D	To 83 or 65	Read cube of dia.	Read diameter
K			Opposite cube of dia.

NOTE.—In this, as in other cases, the coefficients (83 and 65) may be altered to suit individual opinions, without in any way altering the methods of solution.

# To find the Change Wheel in a Screw-Cutting Lathe

$\mathbb{S} \times \mathbb{W}$	(N = Number	of threads	per inch to be cut.
	T = "	44	" on traverse screw.
where	M = "	teeth in	wheel on mandril.
	M = " W = "	**	stud wheel (gearing in M).
$W = NM \times P$	P = "	44	stud wheel (gearing in M). stud pinion (gearing in S).
$\overline{\mathbf{T} \times \mathbf{S}}$	S = "	**	wheel on traverse screw.
- 7, -	(-	1	

C	Set T Ind. to PS	to Ind.	Under M
D	To N		Find No. of teeth in W or stud wheel

Rules for Good Leather Belting  $W = \frac{600 \text{ or } 375 \text{ H. P.}}{V \text{ ft. per min.}}$ 

D	То 600	Find width in inches	Single	Relte
C	Set velocity in feet per min.	Opposite actual H. P.	Diligio	Deite

D	To 375	Find width in inches	Double	Relte
C	Set velocity in feet per min.	Opposite actual H. P.	Dodbie	Deire

# Best Manila Rope Driving

A	To velocity in feet per min.	Find Actual Horse Power
В	Set 307	
C		Above diameter in inches
		1000

A	To 4	Find Strength in Tons
В		ı.
C	Set 1	Above diameter in inches
D		
A	To 107	Find Working Tension in Pounds
В		
C	Set 1	Above diameter in inches
D		
A.	To 0.28	Find Weight per Foot in Pounds
В		<u>.</u>
C	Set 1	Above diameter in inches
D		

# Weight of Iron Bars in Pounds per Foot Length

A	<b>T</b> o 3	Weight of Square Bars
В	Set 1	
C		Above width of side in inches
D		
A	To 55	Weight of Round Bars
В	Set 21	
C		Above diameter in inches
D		

<b>C</b>	Set 0.3	Below thickness in inches				
$\overline{\mathbf{D}}$	Breadth in inches	Weight of Flat Bars				

# Weight of Iron Plates in Pounds per Square Foot

C	Set 32	Below thickness in thirty-seconds of an inch		
D	To 40	Find weight in pounds per square foot		

# Weights of other Metals

C	Set 1	Below G. P. for other metals			
	To weight in iron	Find weight in other metals			

Gauge-points of other metals, and weight per cubic foot.

	Cast			Steel			Cast		
477	W. I.	C. I.	Steel.	Plates.	Copper.	Brass.	Lead.	Zinc.	
G. P	1	.93	1.02	1.04	1.15	1.09	1.47	.92	
Weight	480	450	490	500	550	525	710	440 pounds	

Example: What is the weight of a bar of copper, 1 foot long, 3 inches broad and 2 inches thick?

C   Set 0.3		R to 2 inches thick	1 to R	Below G. P. 1.15
	To 3 inches broad			Find 23 pounds—Ans.

# Weight of Cast Iron Pipes

С	Set .4075	Below Difference of inside and outside diameters in inches			
D	To Sum of inside and outside diameters in inches	Find weight in pounds per lineal foot			

G. P. for other metals	Brass.	Copper.	Lead.	W. Iron	
		.333			

#### Safe Load on Chains

A		Safe load in tons
В	Set 36 for open link or 28 for stud-link	Above 1
C	or 20 for stud-link	
D	To diameter in sixteenths of an inch	

### Gravity

$\mathbf{C}$	Set 1	Below 32.2			
D	To seconds	Velocity in feet per second			

A	Space fallen through in feet	
В		
C	Set 1	Under 8
D		Velocity in feet per second

A		Space fallen through in ft.
В	32.07.60	Above 16.1
C	Set 1	
$\overline{\mathbf{D}}$	To seconds	

#### Oscillations of Pendulums

A		1
В	Set length pendulum in in.	
C	19	Below 1
D	То 375	Number oscillations per minute

# Comparison of Thermometers

C	Set 5	Degrees Centigrade		
D	То 9	Degrees Fahrenhelt — 32		
C	Set 4	Degrees Reaumur		
D	То 9	Degrees Fahrenheit — 32		
D	То 9	Degrees Fahrenheit — 3		
		et 4 Degrees Reaumur		
	$\mathbf{D} \parallel \mathbf{T}$	o 5 Degrees Centigrade		

#### Force of Wind

A	To 66	Find pressure in pounds per square foot
В	R. Index	
$\mathbf{C}$		Velocity in Feet per second
D		
A	To 45	Find pressure in pounds per square foot
В	R. Index	
$\mathbf{C}$		Velocity in Miles per hour
D		

## Discharge from Pumps

_A_		Gallons delivered per stroke
В	Set 294	Stroke in inches
c		
D	To diameter in inches	

# Diameter of Single-acting Pumps

A	To 294			
В	Set length of stroke in inches	R to gallons to be delivered per min.	No. strokes per	· · · · · · · · · · · · · · · · · · ·
C	in inches	denvered per min.	min. to R	Below 1
D				Diam. pump in inches

### Horse Power required for Pumps

C	Set G. P.	Height in feet to which the water is to be raised
D	To cubic feet or gallons to be raised per minute	Horse power required

# Gauge Points with different percentages of allowance.

Per Cent						60		80
For Gallons Im	p3300 3000	2750	2540	2360	2200	2060	1940	1835
" C. Feet	528 480	440	406	377	352	330	311	294
" U.S. Gallor	ns3960 3600	3300	3050	2830	2640	2470	2330	2200

# Theoretical Velocity of Water for any Head

A	Head in feet	
В		
С	Set 1	Under 8
D		Velocity in feet per second

#### Theoretical Discharge from an Orifice 1 inch Square

A	,		}
В	Set 1	Under head in feet	If the hole is round and one inch dia.
С			the G. P. is 2.62
D	To G. P. 3.34	Discharge in cubic feet per minute	}

### Real Discharge from Orifice in a Tank 1 inch Square

A			
В	Set 1	Under head in feet	If the hole is round and 1 inch diam.,
C	W 2770		the G. P. is 1.65
D	To 2.1 G. P.	Discharge in cubic feet per minute with coefficient .63	

#### Gauge Points for other coefficients.

#### Discharge from Pipes when real velocity is known

11	A		Discharge in cubic feet per min.
	$\overline{\mathbf{c}}$		Above 1.75
Inverted {	В	Velocity in feet per second	
	$\overline{\mathbf{q}}$	Diameter in inches	

Delivery	-5	Water	from	Dinge
Delivery	O1	MATCI	HUHH	TIPES

	D <sub>6</sub> H
W = 4.71	L_
Eytelwein	's Rule

L	Read log of dia.	$Log dia \times 5 = x$	STR. STEVEN GOVERNOUS GOVERNMENT	
D	Opp.dia.in inch.			Read cu.ft. per min.
A		Opposite x		
В		Set length in feet	Opp. head in feet	
$\mathbf{c}$			Set index	Opposite 4 71
			,	

When setting x on A do not include characteristic

	. A	ľ	Ì	Gaug	ing V	Vate	r w	ith a	Weir			
7	$\int \overline{\mathbf{c}}$	-			_	-					-	
Invert	ed B	De	pth in	inche	U	nder	4.3					
	D (	De	pth in	inche	3 D	ischa	ırge	in cu	bic fee	t per	min	ute from
							ea	ich 100	t widt		ill H	≺ V
		I	Discha			arbii	ne				0.	= D
	( <del></del>	<u> </u>	He	ad in	feet		_ _					
	B	<b> </b>	•									
	( <u>c</u>						U	Inder s	quare	inches	wat	ter vented
	D	[]		0.3						scharg	ed p	er minute
	ш. т		1	Revo	lutio 	ns o	fa	Turbi	ne			
A	To hea	a in i	eet				<u> </u>					·
B												
C Set	diamet	er in	inches	R to 1	840 1	to R	ļυ	nder r	ate of	perip	пега	l velocity
D			Ì			1000	Ì	Find	revol	utions	per	min.
11			] ]-	lorse	Powe	er of	   • 1	ľurbir				
С	Set 530	) F	to dis						I	R	Perc isefu	entage il effect
$\mathbf{D} \parallel \mathbf{I}$	Head in						88			H	orse	power
A	Und head											
or, C	Set	1	R i		158 t	o R	Ve	R to		to R		Under
			-		100 t			ill ill s	q. m.	to K	-	ful effect
_		,	Ho	se Po	wer	of a	Ste	am Ei	ngine	,	110	rse power
	Set 1,000 d	R to liam.	1 to R	R	to	1		R to	rev	to R		pressure
	diam.										Hors	se power
 A	•	1		•		1			t	1	1	н. Р.
or, B	Set 21,0	000 1	R to st	roke i	n ft.	1 to	R		R to utions	1to	R	Mean pressure
D	To dia in incl								25		_	

#### Dynamometer; to Estimate the indicated H. P.

C	Set 5252	R to length of lever in feet from center of shaft	Under rev. of shaft per min.
D	Weight applied at end of lever in pounds, including weight of scale		Actual horse power

To find the Geometric Mean, or Mean Proportional between two numbers' or a:x::x:b

A		
В	Set less No. a	Below b
C		
$\overline{\mathbf{D}}$	To less No. a	Find $X = G$ , M

NOTE.—In operations involving square root care should be taken to move the decimal point an even number of places and to use the proper right or left half of A or B.

To reduce fractions to decimals:

C	Set numerator	Find equivalent decimal
$\overline{\mathbf{D}}$	To denominator	Above 1
To reduce d	ecimals to fractions:	
C	Set decimal	Find equivalent numerators
D	To 1	Find equivalent denominators

# TABLE OF EQUIVALENTS OR GAUGE POINTS FOR SCALES C AND D

The following equivalents are in the form of proportions, which should be solved as such, thus

Diameters of circles =  $\frac{113}{355}$  Circumferences of circles

Circumferences of circles  $=\frac{355}{113}$  Diameters of circles.

The above are now in a form for ready solution upon the slide rule.

#### GEOMETRICAL

113 = Diameters of circles

355 = Circumferences of circles

79 = Diameter of circle

70 = Side of equal square

99 = Diameter of circle

70 = Side of inscribed square

39 = Circumference of circle

11 = Side of equal square

40 = Circumference of circle

9 = Side of inscribed square

70 = Side of square

99 = Diagonal of square

205 = Area of square whose side = 1

161 = Area of circle whose diameter = 1

322 = Area of circle

205 = Area of inscribed square

#### ARITHMETICAL

100 = Links66 = Feet

12 = Links

95 = Inches

101 = Square links

44 = Square feet

6 = U. S. Gallons

5 = Imperial gallons

1 = U. S. gallons

231 = Cubic inches

800 = U. S. gallons

107 = Cubic feet

22 = Imperial gallons

6100 = Cubic inches

430 = Imperial gallons

69 = Cubic feet

#### METRIC SYSTEM

26 = Inches 66 = Centimeters

82 = Yards

75 = Meters

4300 = Links

865 = Meters

82 = Feet25 = Meters

87 = Miles

140 = Kilometers

43 = Chains

865 = Meters

<del>- 74</del>
31 = Square inches
200 = Square Centimeters
140 = Square feet
13 = Square meters
61 = Square yards
51 = Square meters
42 = Acres
17 = Hectares
22 = Square miles
57 = Square kilometers
5 = Cubic inches 82 = Cubic centimeters
600 = Cubic feet
17 = Cubic meters
85 = Cubic yards
65 = Cubic meters
6 = Cubic feet
170 = Liters
14 = U. S. gallons
53 = Liters
46 = Imperial gallons 209 = Liters
6 = Ounces
$\frac{6 = \text{Ounces}}{170 = \text{Grams}}$
$\frac{6 = \text{Ounces}}{170 = \text{Grams}}$ $63 = \text{Hundredweights}$
$ \begin{array}{r} 6 = \text{Ounces} \\ \hline 170 = \text{Grams} \\ 63 = \text{Hundredweights} \\ 3200 = \text{Kilograms} \end{array} $
$\frac{6 = \text{Ounces}}{170 = \text{Grams}}$ $\frac{63 = \text{Hundredweights}}{3200 = \text{Kilograms}}$ $63 = \text{English tons}$
$\frac{6 = \text{Ounces}}{170 = \text{Grams}}$ $\frac{63 = \text{Hundredweights}}{3200 = \text{Kilograms}}$ $63 = \text{English tons}$ $64 = \text{Metric tons}$
$\frac{6 = \text{Ounces}}{170 = \text{Grams}}$ $\frac{63 = \text{Hundredweights}}{3200 = \text{Kilograms}}$ $64 = \text{Metric tons}$ PRESSURES
6 = Ounces 170 = Grams 63 = Hundredweights 3200 = Kilograms 64 = Metric tons  PRESSURES 640 = Pounds per square inch
6 = Ounces 170 = Grams 63 = Hundredweights 3200 = Kilograms 64 = Metric tons PRESSURES 640 = Pounds per square inch 45 = Kilogs per square centimeter
6 = Ounces 170 = Grams 63 = Hundredweights 3200 = Kilograms 64 = Metric tons PRESSURES 640 = Pounds per square inch 45 = Kilogs per square centimeter
6 = Ounces 170 = Grams 63 = Hundredweights 3200 = Kilograms 64 = Metric tons  PRESSURES 640 = Pounds per square inch 45 = Kilogs per square centimeter 51 = Pounds per square foot 249 = Kilogs per square meter
6 = Ounces 170 = Grams 63 = Hundredweights 3200 = Kilograms 64 = Metric tons PRESSURES 640 = Pounds per square inch 45 = Kilogs per square centimeter
6 = Ounces 170 = Grams 63 = Hundredweights 3200 = Kilograms 64 = Metric tons  PRESSURES 640 = Pounds per square inch 45 = Kilogs per square centimeter 51 = Pounds per square foot 249 = Kilogs per square meter 59 = Pounds per square yard 32 = Kilogs per square meter 57 = Inches of mercury
6 = Ounces  170 = Grams  63 = Hundredweights  3200 = Kilograms  64 = Metric tons  PRESSURES  640 = Pounds per square inch  45 = Kilogs per square centimeter  51 = Pounds per square foot  249 = Kilogs per square meter  59 = Pounds per square yard  32 = Kilogs per square meter  57 = Inches of mercury  28 = Pounds per square inch
6 = Ounces 170 = Grams 63 = Hundredweights 3200 = Kilograms 64 = Metric tons PRESSURES 640 = Pounds per square inch 45 = Kilogs per square centimeter 51 = Pounds per square foot 249 = Kilogs per square meter 59 = Pounds per square yard 32 = Kilogs per square meter 57 = Inches of mercury 28 = Pounds per square inch 82 = Inches of mercury
6 = Ounces  170 = Grams  63 = Hundredweights  3200 = Kilograms  64 = Metric tons  PRESSURES  640 = Pounds per square inch  45 = Kilogs per square centimeter  51 = Pounds per square foot  249 = Kilogs per square meter  59 = Pounds per square meter  59 = Pounds per square meter  57 = Inches of mercury  28 = Pounds per square inch  82 = Inches of mercury  5800 = Pounds per square foot
6 = Ounces  170 = Grams  63 = Hundredweights  3200 = Kilograms  64 = Metric tons  PRESSURES  640 = Pounds per square inch  45 = Kilogs per square centimeter  51 = Pounds per square foot  249 = Kilogs per square meter  59 = Pounds per square meter  59 = Pounds per square meter  57 = Inches of mercury  28 = Pounds per square inch  82 = Inches of mercury  5800 = Pounds per square foot  720 = Inches of water
6 = Ounces 170 = Grams 63 = Hundredweights 3200 = Kilograms 64 = Metric tons PRESSURES 640 = Pounds per square inch 45 = Kilogs per square centimeter 51 = Pounds per square foot 249 = Kilogs per square meter 59 = Pounds per square meter 59 = Pounds per square meter 57 = Inches of mercury 28 = Pounds per square inch 82 = Inches of mercury 5800 = Pounds per square foot 720 = Inches of water 26 = Pounds per square inch
6 = Ounces  170 = Grams  63 = Hundredweights  3200 = Kilograms  64 = Metric tons  PRESSURES  640 = Pounds per square inch  45 = Kilogs per square centimeter  51 = Pounds per square foot  249 = Kilogs per square meter  59 = Pounds per square meter  59 = Pounds per square meter  57 = Inches of mercury  28 = Pounds per square inch  82 = Inches of mercury  5800 = Pounds per square foot  720 = Inches of water
6 = Ounces  170 = Grams  63 = Hundredweights  3200 = Kilograms  64 = Metric tons  PRESSURES  640 = Pounds per square inch  45 = Kilogs per square centimeter  51 = Pounds per square foot  249 = Kilogs per square meter  59 = Pounds per square meter  59 = Pounds per square meter  57 = Inches of mercury  28 = Pounds per square inch  82 = Inches of mercury  5800 = Pounds per square foot  720 = Inches of water  26 = Pounds per square inch  74 = Inches of water

 $\frac{108 = Grains}{7 = Grams}$ 

75 = Pounds 34 = Kilograms

5 = Feet of water
312 = Pounds per square foot
15 = Inches of mercury 17 = Feet of water
17 = Feet of water
99 = Atmospheres
2960 = Inches of mercury
34 = Atmospheres
500 = Pounds per square inch
34 = Atmospheres
7200 = Pounds per square foot
30 = Atmospheres
31 = Kilogs per square centimeter
23 = Atmospheres
780 = Feet of water
3 = Atmospheres
31 = Meters of water
29 = Pounds per square inch
67 = Feet of water
1 = Kilogs per square centimeter
10 = Meters of water
COMBINATIONS
49 - Pounds now foot
43 = Pounds per foot 64 = Kilogs per meter
64 = Kilogs per meter
64 = Kilogs per meter 127 = Pounds per yard
64 = Kilogs per meter 127 = Pounds per yard 63 = Kilogs per meter
64 = Kilogs per meter 127 = Pounds per yard 63 = Kilogs per meter 46 = Pounds per square yard
64 = Kilogs per meter 127 = Pounds per yard 63 = Kilogs per meter 46 = Pounds per square yard 25 = Kilogs per square meter
64 = Kilogs per meter 127 = Pounds per yard 63 = Kilogs per meter 46 = Pounds per square yard 25 = Kilogs per square meter 49 = Pounds per cubic foot
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter
64 = Kilogs per meter 127 = Pounds per yard 63 = Kilogs per meter 46 = Pounds per square yard 25 = Kilogs per square meter 49 = Pounds per cubic foot
64 = Kilogs per meter 127 = Pounds per yard 63 = Kilogs per meter 46 = Pounds per square yard 25 = Kilogs per square meter 49 = Pounds per cubic foot 785 = Kilogs per cubic meter 27 = Pounds per cubic yard
64 = Kilogs per meter 127 = Pounds per yard 63 = Kilogs per meter 46 = Pounds per square yard 25 = Kilogs per square meter 49 = Pounds per cubic foot 785 = Kilogs per cubic meter 27 = Pounds per cubic yard 16 = Kilogs per cubic meter 89 = Cubic feet per minute 42 = Liters per second
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second  840 = U. S. gallons per minute
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second  840 = U. S. gallons per minute  53 = Liters per second
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second  840 = U. S. gallons per minute  53 = Liters per second  840 = U. S. gallons per minute
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second  840 = U. S. gallons per minute  53 = Liters per second  840 = Weight of fresh water  39 = Weight of sea water
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second  840 = U. S. gallons per minute  53 = Liters per second  38 = Weight of fresh water  39 = Weight of sea water  5 = Cubic feet of water
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second  840 = U. S. gallons per minute  53 = Liters per second  38 = Weight of fresh water  59 = Weight of sea water  5 = Cubic feet of water  312 = Weight in pounds
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second  840 = U. S. gallons per minute  53 = Liters per second  38 = Weight of fresh water  39 = Weight of sea water  5 = Cubic feet of water  312 = Weight in pounds  1 = Imperial gallons of water
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second  840 = U. S. gallons per minute  53 = Liters per second  38 = Weight of fresh water  39 = Weight of sea water  5 = Cubic feet of water  312 = Weight in pounds  1 = Imperial gallons of water  10 = Weight in pounds
64 = Kilogs per meter  127 = Pounds per yard  63 = Kilogs per meter  46 = Pounds per square yard  25 = Kilogs per square meter  49 = Pounds per cubic foot  785 = Kilogs per cubic meter  27 = Pounds per cubic yard  16 = Kilogs per cubic meter  89 = Cubic feet per minute  42 = Liters per second  700 = Imperial gallons per minute  53 = Liters per second  840 = U. S. gallons per minute  53 = Liters per second  38 = Weight of fresh water  39 = Weight of sea water  5 = Cubic feet of water  312 = Weight in pounds  1 = Imperial gallons of water

5	0 = Pounds per U. S. gallon
	6 = Kilogs per liter
	0 = Pounds per Imperial gallon
	1 = Kilogs per liter
	0 = Pounds per U. S. gallon
$\overline{}_2$	5 = Pounds per Imperial gallon
	3 = Cubic feet of water
8	5 = Weight in kilogs
	6 = Imperial gallons of water
20	9 = Weight in kilogs
	4 = U. S. gallons of water
	3 = Weight in kilogs
	4 = Feet per second
3	0 = Miles per hour
8	8 = Yards per minute
	3 = Miles per hour
	1 = Feet per second
	0 = Meters per minute
	2 = Feet per minute
	5 = Meters per minute
	0 = Footpounds
	7 = Kilogrammeters
	2 = British horse power
7	3 = French horse power

3700 = One cubic foot of water per minute under one foot of head

7 = British horse power

75 = One liter of water per second under one meter of head

1 = French horse power

In no case does the departure, in these equivalents, from the exact ratio attain one per thousand.

#### **EXAMPLES**

What is the pressure in pounds per square inch equivalent to a head of 31 feet of water.

C	Set 60	Under 34
$\overline{\mathbf{p}}$	To 26	Find 14.75 pounds—Answer

What head of water, in feet, is equivalent to a pressure of 18 pounds per square inch.

$\mathbf{C} \parallel$	Set 26	Under 18
$\overline{\mathbf{D}}$	То 60	Find 4I.5 feet—Answer

How many horse power will 50 cubic feet of water per minute give under a head of 400 feet.

C	Set 3700	Runner to 400	1 to R	Under 50
$\overline{\mathbf{D}}$	To 7.		5.	Find 37.8 H. P.—Answer

#### SUMMARY OF CONVENIENT SETTINGS

In the following problems and formulas a, b, and c represent any numbers and x the unknown quantity or answer sought. For the purpose of illustration only simple numbers are used in the examples. It will be noted that most of the problems may be solved in two ways, i. e., different sets of scales may be used. However, the scales must be selected that will keep at least half of the slide within the scales on the body of the rule.

# Multiplication and Division of Three Quantities, One of which is Variable

 $x = \frac{a \ c}{b} = \frac{4 \ c}{16}$ 

Example:  $x = \frac{a}{c} = \frac{75 \times 8}{c}$ Set 8 on CIF to 75 on DF, at any value of c on  $\begin{cases} \text{CIF, find } x \text{ on DF} \\ \text{CI, find } x \text{ on D} \end{cases}$ 

 $x = \frac{a}{b \ c} = \frac{84}{12 \times c}$ Example:

Set 12 on CF to 84 on DF, at any value of c on  $\begin{cases} CIF, & \text{find } x \text{ on DF} \\ CI, & \text{find } x \text{ on D} \end{cases}$ 

# Multiplication and Division of Four Quantities, One of which is $\pi$ with one setting of slide

 $x = \pi abc = \pi \times 5 \times 8 \times 3$ Example:

Set 8 on CIF to 5 on D, at 3 on C find 377 on D, or at 3 on CF find 377

Any product or quotient which could be read on CF or DF, may be divided by  $\pi$  merely by reading on D or C.

 $x = \frac{abc}{\pi} = \frac{35 \times 4 \times c}{\pi}$ Example:

Set 4 on CI to 35 on D. at values of c on CF read x on D.

 $x = \frac{a.b}{c.\pi} = \frac{8 \times 9}{c \times \pi}$ Example:

Set 9 on CIF to 8 on DF, at values of c on CIF read x on D.

#### EXPRESSIONS WHICH MAY BE READ DIRECTLY

#### by Means of the Indicator, without Setting the Slide

#### HIGHER POWERS AND ROOTS

The fourth root of a number is obtained by finding the square root of the square root. The sixth root is obtained by finding the square root of the cube root. The eighth root is the square root of the fourth root.

- 1.  $x = a^2$ , set Indicator to a on D, read x on A.
- 2.  $x = a^3$ , set Indicator to a on D,
- 3.  $x = \sqrt{a}$ , set Indicator to a on A, read x on D.
- 5.  $x = \sqrt{a^3}$ , set Indicator to a on A, read x on K.
- 6.  $x = \sqrt[3]{a^2}$ , set Indicator to a on K,
- read x on C.
- read x on D.
- 10.  $x = \frac{\pi}{a}$ , set Indicator to a on CF, read x on CI.
- 11.  $x = \frac{1}{a \times \pi}$ , set Indicator to a on C, read x on CIF.
- 12.  $x = \pi \sqrt{a}$ , set Indicator to a on A, read x on DF.
- 13.  $x = \pi \sqrt[3]{a}$ , set Indicator to a on K. read x on DF.
- read x on A.

- 15.  $x = \frac{a^3}{3}$ , set Indicator to a on DF read x on K.
- 16.  $x = \pi \sqrt{\sin a}$ , set Indicator to a on S, read x on CF.
- 4.  $x = \sqrt[4]{a}$ , set Indicator to a on K, 17.  $x = \frac{1}{\sqrt{\sin a}}$ , set Indicator to a on S, read x on CIF.
  - 18.  $x = \pi \tan a$ , set Indicator to a on T, read x on CF.
- 7.  $x = \frac{1}{a}$ , set Indicator to a on CI, 19.  $x = \frac{1}{\pi \tan a} = \frac{\cot a}{\pi}$ , set Indicator
- 8.  $x = a \times \pi$ , set Indicator to a on D, 20.  $x = \frac{1}{\tan a} = \cot a$ , set Indicator to read x on DF. a on T. read x on CI.
- 9.  $x = \frac{a}{\pi}$ , set Indicator to a on DF, 21.  $x = \log a$ , set Indicator to a on D, read x on L.
  - 22.  $x = \log \sqrt{a}$ , set Indicator to a on A. read x on L.
  - 23.  $x = \log \sqrt[3]{a}$ , set Indicator to a on K. read x on L.
  - 24.  $x = \log \frac{a}{x}$ , set Indicator to a on DF. read x on L.
  - 25.  $x = \frac{1}{a^2}$ , set Indicator to a on CI, read x on B.
- 14.  $x = \frac{a^2}{a^2}$ , set Indicator to a on DF, 26.  $x = \frac{1}{\sqrt{a^2}}$ , set Indicator to a on B, read x on CI.

### EXPRESSIONS WHICH MAY BE READ DIRECTLY

# by Means of the Indicator, without Setting the Slide

With indices in alignment.

27.  $x = \tan a$ , set Indicator to a on T, read x on D.

28.  $x = -\frac{1}{a^3}$ , set Indicator to a on CI, read x on K.

30.  $x = \frac{1}{-3 a^3}$ , set Indicator to a on CIF, read x on K.

31.  $x = \frac{1}{a^3/a}$ , set Indicator to a on K. read x on CI.

32.  $x = \frac{1}{\pi \sqrt{a}}$ , set Indicator to a on

29.  $x = \frac{1}{x^2 a^2}$ , set Indicator to a on CIF, 33.  $x = \frac{1}{x^{2/a}}$ , set Indicator to a on

#### EXPRESSIONS SOLVED AT ONE SETTING OF SLIDE

#### ONE FACTOR

34.  $x = a^4$ , set 1 to a on D, at a on C, read x on A.

35.  $x = \frac{1}{x^2}$ , set a on CI to a on D, under 1 on A. read x on B.

36.  $x = a^5$ , set a on CI to a on D, over a on B, read x on A.

37.  $x = \frac{1}{a^5}$ , set a on C to a on K, at a on CI, read x on K.

38.  $x = a^6$ , set 1 on C to a on D, at a on C read x on K.

39.  $x = a^7$ , set a on CI to a on K, at a on C read x on K.

40,  $x = a^9$ , set a on CI to a on D, at a on C read x on K.

41.  $x = \sqrt{a^5}$ , set 1 to a on K, at a on B, read x on K.

43.  $x = \sqrt{a^{11}}$ , set a on CI to a on K, at a on B, read x on K,

44.  $x = \sqrt{a^{16}}$ , set a on CI to a on D, at a on B, read x on K.

45.  $x = \frac{1}{\sqrt[3]{a^2}}$ , set 1 to a on K, at 1 on A, read x on B.

46.  $x = \sqrt[3]{a^4}$ , set 1 to a on K, at a on C read x on D.

47.  $x = \frac{1}{\sqrt[3]{a^4}}$ , set a on CI to a on K, at 1 on D read x on C.

48.  $x = \sqrt[3]{a^5}$ , set 1 to a on K, at a on B, read x on A.

49.  $x = \frac{1}{a^3/a^6}$ , set *a* on C to *a* on K, at a on CI read x on D.

50.  $x = \sqrt[3]{a^7}$ , set a on CI to a on K, at a on C read x on D.

51.  $x = \sqrt[3]{a^8}$ , set 1 to a on K, at a on C read x on A.

42.  $x = \sqrt{a^9}$ , set 1 to a on A, at a on 52.  $x = \frac{1}{\sqrt[3]{a^8}}$ , set a on CI to a on K, at 1 on A, read x on B.

> 53.  $x = \frac{1}{\sqrt[4]{a^{10}}}$ , set *a* on C to *a* on K, at a on CI read x on A.

- 54.  $x = \sqrt[3]{a^{11}}$  set a on CI to a on K, 58.  $x = \sqrt[6]{a^5}$ , set 1 to a on K, at a on over a on B read x on A.
- 55.  $x = \sqrt[3]{a^{14}}$ , set a on CI to a on K, at a on C, read x on A.
- 59.  $x = \sqrt[6]{a^7}$ , set a on B to a on K, at a on D, read x on C.
- 56.  $x = \sqrt[6]{a}$ , set a on B to a on K, at 60.  $x = \frac{1}{\sqrt[6]{a^7}}$ , set a on B to a on K, 1 on D read x on A.
- 57.  $x = \frac{1}{\sqrt[6]{a}}$ , set a on B to a on K, at 1 on C read x on D.
- at a on D read x on CI. 61.  $x = \sqrt[6]{a^{11}}$ , set a on CI to a on K, at a on B, read x on D.

#### SETTINGS FOR TWO FACTORS

- 62. x = ab, set 1 to a on D, under b on C read x on D.
- 72.  $x = \frac{1}{a^3 h^3}$ , set a on C to 1 on D, over b on CI, read x on K.
- 63.  $x = \frac{1}{ab}$ , set a on CI to b on D, over 1 on D read x on C.
- 73.  $x = \frac{a^2}{b^2}$ , set b on C to a on D, over 1 on C, read x on A.
- 64.  $x = \frac{a}{b}$ , set b on C to a on D, under 74.  $x = a\sqrt{a}$ , set 1 on C to b on A, under a on C read x on D. 1 on C read x on D.
- 65. =  $\frac{1}{a}$ , set b on C to a on D, over 1 on D read x on C.
- 75.  $x = \frac{1}{a\sqrt{b}}$ , set on a CI to b on A, over D read x on C.
- 66.  $x = ab^2$ , set 1 to a on A, over b on C read x on A.
- 76.  $x = \frac{\sqrt{a}}{b}$ , set b on C to a on A, under 1 on C read x on D.
- 67.  $x = \frac{1}{a^2}$ , set b on CI to a on A, under 1 on A read x on B.
- 77.  $x = \frac{a}{\sqrt{b}}$ , set b on B to a on D, under 1 on CI read x on D.
- 68.  $x = \frac{a}{h^2}$ , set b on C to a on A, over 1 on B read x on A.
- 78.  $x = \sqrt[3]{b}$ , set a on CI to a on D, 11 ser b on B read x on D. 79. x = a set a on CI to b on A,
- 69.  $x = \frac{a^2}{b}$ , set a on C to b on A, under 1 on A read x on B.
- 80.  $x = a^5 \sqrt{b^3}$  set a on CI to b on A, over 1 on C read x on K.

over a on C read x on A.

- 70.  $x = a^2 b^2$ , set 1 on C to a on D, over b on C read x on A.
- 81.  $x = \frac{a^2}{\sqrt{b}}$ , set b on B to a on D, over a on C read x on D.
- over b on CI, read x on A.
- 71.  $x = \frac{a^2}{a^2 k^2}$ , set a on C to 1 on D, 82.  $x = \frac{\sqrt{a}}{k^2}$ , set b on C to a on A, under b on CI, read x on D.

- 83.  $x = ab^3$ , set 1 on C to a on K, at b on C, read x on K.
- 84.  $x = -\frac{a}{ha}$ , set b on C to a on K, at 1 on C, read x on K.
- 85.  $x = \frac{a^2}{1.2}$ , set a on CI to a on A, over b on CI, read x on A.
- 86.  $x = \frac{a^2}{a^2}$ , set b on B to a on D, over b on CI, read x on A.
- 87.  $x = a^2 b^3$ , set b on CI to a on D, over b on B, read x on A.
- 88.  $x = a \sqrt[3]{b}$ , set 1 on C to b on K, under a on C, read x on D.
- 89.  $x = \frac{1}{a\sqrt[3]{b}}$ , set a on CI to b on K, over 1 on D, read x on C.
- over 1 on D, read x on C.

- 91.  $x = \frac{\sqrt[3]{a}}{b}$ , set b on C to a on K, under 1 on C, read x on D.
- 92.  $x = a^3 b^3$ , set 1 on C to b on D, at a on C, read x on K.
- 93.  $x = \frac{a^3}{b^3}$ , set b on C to a on D, at 1 on C read x on K.
- 94.  $x = ab^4$ , set b on CI to a on A, over b on C, read x on A.
- 95.  $x = b^6 \sqrt{a^3}$ , set b on CI to a on A, at b on C, read x on K.
- 96.  $x = a^2 \sqrt[3]{b^2}$ , set 1 on C to b on K, under a on C, read x on A.
- 97.  $x = \frac{\sqrt[3]{a^4}}{b}$ , set b on C to a on K, under a on C read x on D.
- 98.  $x = \frac{\sqrt[3]{a^8}}{1.5}$ , set b on C to a on K, over a on C, read x on A.
- 90.  $x = \frac{a}{\sqrt[3]{h}}$ , set a on C to b on K, 99.  $x = \frac{a^4}{h^3}$ , set b on C to a on K, over a on C, read x on K.

#### SETTINGS FOR TWO FACTORS AND T

- 100.x = a. b.  $\pi$ , set i on C to a on D, over b on C, read x on DF.
- $101.x = \frac{\pi}{a \ b}, \text{ set } a \text{ on CI to } b \text{ on D,}$ over 1 on D, read x on CF.
- $102.x = \frac{a \ b}{\pi}$ , set a on CI to b on D, over 1 on D, read x on CIF.
- $103.x = \frac{\pi^2 a}{b^2}, \text{ set } b \text{ on CF to } a \text{ on A},$ over 1 on C, read x on A.
- $104.x = \frac{\pi\sqrt{a}}{b}, \text{ set } b \text{ on CF to } a \text{ on A,}$ under 1 on C, read x on D.
- $105.x = \frac{\pi^2}{a^2 b^2}, \text{ set } a \text{ on CF to 1 on D,}$ over b on CI, read x on A.
- $106.x = \frac{\pi^{\delta}}{a^2 b^3}, \text{ set } a \text{ on CF to 1 on D,}$ over b on CI, read x on K.
- $107.x = \frac{\pi^2}{b^2}, \text{ set } b \text{ on CF to 1 on D,}$ over a on C, read x on A.
- $108.x = \frac{\pi^3 \ a^3}{b^3}, \text{ set } b \text{ on CF to 1 on D,}$ over a on C, read x on K,
- $109.x = \frac{a}{\pi b}, \text{ set 1 on C to } a \text{ on D,}$ under b on CIF, read x on D.
- $110.x = \frac{a^3}{\pi^2 b^2}, \text{ set 1 on C to } a \text{ on D,}$ over b on CIF, read x on A.
- 111.x =  $\frac{a^3}{\pi^3 b^3}$ , set 1 on C to a on D, over b on CIF, read x on K.
- 112.x =  $\pi$   $a^2\sqrt{b}$ , set a on CI to b on A, over a on C, read x on DF.
- 113.x =  $\frac{\pi a}{\sqrt{b}}$ , set a on C to b on A, over 1 on D, read x on CF.

- $114.x = \frac{\sqrt{b}}{\pi a}, \text{ set } a \text{ on C to } b \text{ on A},$ over 1 on D, read x on CIF.
- 115.x =  $\frac{\pi a^2}{\sqrt{b}}$ , set a on C to b on A, over a on D, read x on CF.
- 116.x =  $\frac{\sqrt{b}}{\pi a^2}$ , set a on C to b on A, over a on D, read x on CIF.
- $117.x = \frac{\pi \sqrt[3]{a}}{b}, \text{ set } b \text{ on C to } a \text{ on K,}$ over 1 on C, read x on DF.
- 118.x =  $\pi \sqrt{a^5}$ , set a on CI to a on A, over a on C, read x on DF.
- 119.x =  $\pi \sqrt[3]{a^4}$ , set 1 to a on K, over a on C, read x on DF.
- $120.x = \frac{\pi}{\sqrt[3]{a^4}}, \text{ set } a \text{ on CI to } a \text{ on K,}$ over 1 on D, read x on CF.
- 121.x =  $\frac{\pi}{\sqrt[3]{a^5}}$ , set a on C to a on K, over a on CI, read x on DF.
- 122.x =  $\pi \sqrt[3]{a^7}$ , set a on CI to a on K, over a on C, read x on DF.
- 123.x =  $\frac{\pi}{\sqrt[3]{a^2}}$ , set a on C to a on K, at 1 on C, read x on DF.
- 124.x =  $\frac{\pi}{\sqrt[3]{a^5}}$ , set a on C to a on K, at a on CI, read x on DF.
- $125.x = \frac{\pi\sqrt[3]{a^4}}{b}, \text{ set } b \text{ on C to } a \text{ on K,}$ over a on C, read x on DF.
- 126.x =  $\frac{\pi}{a\sqrt[4]{b}}$ , set a on CI to b on K, over 1 on D, read x on CF.
- $127.x = \frac{a\sqrt[3]{b}}{\pi}, \text{ set } a \text{ on CI to } b \text{ on K,}$ over 1 on D, read x on CIF.

#### SETTINGS FOR THREE FACTORS

- 128.x = a. b. c, set a on CI to b on D, under c on C, read x on D.
- 129.x =  $a^2 \times b^2 \times c^2$ , set a on CI to b on D, over c on C, read

- 130.  $x = a^2 \times b^3 \times c^2$ , set a on CI to b on D, over c on C, read x on K.
- 131.  $x = \frac{a \times b}{c}$ , set c on C to a on D, under b on C, read x on D.
- 132.  $x = \frac{a^2 b^2}{c^2}$ , set c on C to a on D, over b on C, read x on A.
- 133.  $x = \frac{a^3 b^2}{c^3}$ , set c on C to a on D, over b on C, read x on K.
- 134.  $x = \frac{a}{bc}$ , set b on C to a on D, under c on CI, read x on D.
- 135.  $x = \frac{a^2}{b^2 \times c^2}$ , set b on C to a on D, over c on CI, read x on A.
- 136.  $x = \frac{a^3}{b^3 \times c^9}$  set b on C to a on D, over c on CI, read x on K.

- 137.  $x = a b \sqrt{c}$ , set a on CI to c on A, under b on C, read x on D.
- 138.  $x = a^2 b^2 c$ , set a on CI to c on A, over b on C, read x on A.
- 139.  $x = a^3b^2\sqrt{c^3}$ , set a on CI to c on A, over b on C, read x on K.
- 140.  $x = a \ b \ \sqrt[3]{c}$ , set a on CI to c on K, under b on C, read x on D.
- 141.  $x = a^2 b^2 \sqrt[3]{c^2}$ , set a on CI to c on K, over b on C, read x on A.
- 142.  $\mathbf{x} = a^3 b^3 c$ , set a on CI to c on K, over b on C, read x on K.
- 143.  $x = \frac{\sqrt{a}}{b\sqrt[3]{c}}$ , set b on CI to c on K, under a on A, read x on C.
- 144.  $x = \frac{a\sqrt{b}}{\sqrt[3]{c}}$ , set a on C, to c on K, under b on A, read x on C.

And scores of other combinations.

#### SETTINGS FOR THREE FACTORS AND $\pi$

- 145.  $x = a b c \pi$ , set a on CI to b on D, over c on C, read x on DF.
- 146.  $x = \frac{a b \pi}{c}$ , set c on C to a on D, over b on C, read x on DF.
- 147.  $\mathbf{x} = \frac{a \pi}{b c}$ , set b on C to a on D, over c on CI, read x on DF.
- 148  $x = ab\pi \sqrt{c}$ , set a on CI to c on A, over b on C, read x on DF.
- 149.  $x = ab\pi \sqrt[3]{c}$ , set a on CI to c on K, over b on C, read x on DF.

- 150.  $x = \frac{\pi \sqrt{a}}{b\sqrt[3]{c}}$ , set b on CI to c on K, under a on A, read x on CF.
- 151.  $x = \frac{b\sqrt[3]{c}}{\pi\sqrt{a}}$ , set b on CI to c on K, under a on A, read x on CIF.
- 152.  $x = \frac{\pi a \sqrt{b}}{\sqrt[3]{c}}$ , set a on C to c on K, under b on A, read x on CF.
- 153.  $x = \frac{\sqrt[3]{c}}{\pi a \sqrt{b}}$ , set a on C to c on K, under b on A, read x on CIF.

### ANSWERS.

(Answers given with the problems are	not given	below.)
1. 300.	5.	.03
2. 3000.	6.	3.
3. 3000.	7.	.0003
A 3		

		21	22	28	24	25	26	27	28	29
	31	651	682	713	744	775	806	837	868	899
3	32	672	704	736	768	800	832	864	896	928
	33	693	726	759	792	825	858	891	924	957
	34	714	748	782	816	850	884	918	952	986

		000 0000 10	
9.	49%	41. 74.8	
10.	33%	42. 76200.	
11.	91 %	43. 1170.	
12.	5069	44436	
13.	1607	450039	
10.	33% 91% 59% 16% 21%	4600003	95
14.	21%	4700059	
15.	2.24	40 500000	
16.	2.34	48. 5020000.	
17.	1.33	49. 1.19	
18.	1.32	50. 3.76	
19.	3.18	51. 11.9	
	67.3	<b>52.</b> .376	
21.	19.3	53. 1.56	
22.	.0000476	54. 9.24	
23.	5.77	<b>55.</b> .604	
24.	27.5	56560	
	87.9 In.	57. 38.2	
26.			oots of numbers
	212		10 to 130.
21.	156.	110111	.10 00 100.
28.	.294	37	C D
29.	.735	Number	Square Roots
30.	.615	110.	10.5
31.	13.6	111.	10.5
32.	77.9	112.	10.6
33.	19.6	113.	10.6
34.	21.4	114.	10.7
35.	33.1	115.	10.7
36.	56.7	I16.	10.8
37.	1.6 mils.	117.	10.8
38.	10.2	118.	10.9
39.	21.6	119.	10.9
		120.	11.0
40.	1.25	120.	11.0

			00 —					
1 1	22. 23.	11.0 11 0 11.1 11.1	61.	pi		ches he nea	(Use a 9- arest stand	
		11.2	Ans	swers	to	test	problems	on
		11.2	Page 19					
1 1	28. 29. 30. 127 feet, 3 ir 1.9 inches.		62. 63. 64. 65. 66.	1.4 11.4 36.8	1		Ξ	
		ANSV	VERS.					
		Multip	lication.	o <sup>24</sup>				
67.	7.39		72.	273.				

67. 7.39	72. 273.
68. 19.3 69. 7.55	730541 7400167 750000910
70. 58.5 <b>71. 258.</b>	76. 12.6, 20.4 44.0.
	(A. A. A.

#### Cubes.

77.	2197.	89.	149000.
78.	2744.	90.	262000.
79.	3375.	91.	436,000,000.
80.	4096.	92.	12,500,000.
		93.	77,300,000.
81.	4913.	94.	679,000.
82.	5832.	95.	2,690,000.
83.	6859.		
84.	8000.	96.	.04
85.	9261.	97.	.000185
(Th	ree significant figures).	98.	.000,000,314
<b>86.</b>	29800.	99.	1.09
87.	97300.	100.	9.53
88.	104000.	101.	76.1 gal.

### Cube Roots.

102.	1.44	113.	1.94	
103.	3.107	114.	.002	,
104.	6.69	115.	6.22	
105.	.669	116.	15.66	
106.	.3107	117.	37.34	
107.	.144	118.	.2535	
108.	13.77	119.	.211	
109.	3.628	120.	1.012	
110.	.922	121.	47.7	
111.	35.59	122.	20.4	
112.	9 69			
	UIVU	•		

# Multiplication of More Than Two Numbers. 1.309 56.1

	Manch		
123.	92.4	126.	1.309
124.	114.7	127.	56.1
125.	17,490,000		
	Name of the State	Reciprocals.	
128.	.139	188.	5.49
129.	2.44	134.	.0177
130.	.0265	135.	1.176
	.0147	186.	.136
131.		187.	159.
132.	18.7		

138. 1200. 143. 4.1 139. 46.8 144. 130. 140. 145. 145. 89.1 141. 35.6 146. 107. 142. 157. 147. 63.6  Four and Five Factors.  148. 46.4 151. 1.309 149. 378 152. 56.1	
140. 145	
141. 35.6 142. 157. 147. 63.6 Four and Five Factors. 148. 46.4 151. 1.309	
142. 157. 147. 63.6  Four and Five Factors. 148. 46.4 151. 1.309	
142. 157. 147. 63.6  Four and Five Factors. 148. 46.4 151. 1.309	
148. 46.4 151. 1.309	
1AG 278 159 KC 1	
150. 17,490,000 153. 49.2	
Combined Multiplication and Division.	
15401815 1611585	
155633 <b>162. 4.58</b>	
156. 902. 163. 1.69	
157. 328. 164298	
158. 1111.	
159. 51.4 166. 1.073	
160353	
Miscellaneous Calculations.	
167. 32.3 173. 57,300,000.	
168. 1.91 174. 1.234	
169516 175408	
17045 17600642	
171. 1627. 177. 81.4	
172. 35.8 178. 6.4	
Sines and Cosines.	
179. 1. 194250	
180707 195585	
1815 196937	
182, .0523 1971435	
1830116 1980276	
184264 199. 19.	
1850262 200. 15.1	
1861478 201. 83.2	
1870393 202. 32.0	
1883665 203. 34.5	
1891736 204. 16.3	
190423 205. $a = 9.11, b = 8.04, c = 6$	49.
191748 $d = 5.03$	,
192970 206. $BC = 4.70$ , $BA = 1.71$	
193 .978	
Tangents.	
207466 215270	
208259 2161125	
209713 2170306	
210495 218911	
211335 219. 4.82	
212. 1.446 220. 29.0	
213. 3.78 221. 31.9	
214367 222. 3.04	
Logarithms.	
223127 228. 836.	
224. 1.736 229. 32,600,000,000.	
225. 1.494, or 9.494–10. 230. 1.512	
220. 1.101, 01 0.101 10. 991 9 10	
226. 2.8260, or 8.8260-10.	
227. 2.866	

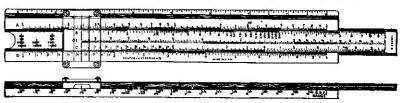
INDEX,		
Accuracy in General, Mufor George 15. 20, 20, 20, 20, 20, 20, 20, 20, 20, 20,	PA	G E
Accuracy in General, 20,	21,	22
Accuracy of Slide Rule,	4—	22
Answers to Problems	85,	86
Belting,		66
Chains,		68
Chemistry,	!	60
Circles	64,	73
Compound Interest	60.	64
Co-ordinates,	!	63
Cosines.	42,	43
Cotangents,		45
Cubes,	27,	28
Cube Root,	29,	30
Cutting Speed,	!	61
Decimal Point, Placing of		8
Decimal Point, Placing of	. • '	72
Discount.	!	59
Division	25,	32
Dynamometer,	• • '	72
Excavating		59
Folded Scales,	7—	79
Formulas,	4—'	72
Fractions, Reduction to Decimals,	!	72
Gearing,	65,	66
Gravity,	!	68
Gauge Points,	3—	76
Higher Powers and Roots.		78
Historical Note.	:	20
Horse Power, Steam Engine.	'	71
Index, which to use,	• •	9
Iron Bars,	• • •	67
Iron Plates,	!	67
Inverted Scale, CI	0	33
Law of Multiplication,	• •	23
Levers,	•_•	65
Logarithms,	47,	48
Mean Proportional,		72
Metal Mixing,		62
Metals, weight of,		67
Miscellaneous Calculations	40,	41
Multiplication, two numbers,	23,	24
Multiplication, three or more numbers,	0-	34
Multiplication, more than three figures,	• •	12
Multiplication, theory,	41	23 77
Multiplication and Division Combined,	41,	70
Orifices, Discharge from	•	40
Patterns,		ÛΙ

,	
Pendulums,	8
Per Cents,	59
Physics,	30
Pipes,	0
Pitch,	55
Proportion,	6
Pulleys,	55
Pumps,	;9
Radians,	
Reading the scales,	2
Reciprocals	9
Rectangular Co-Ordinates,	
Ring,	14
Rope Drive,	6
Safe Load on Chains,	8
Scale CI, Use of	0
Scales, How to Read,	7
Screw-Cutting,	
Secant and Cosecant,	5
Secretarial Work,	9
Selling Price,	4
Shafting,	5
Significant Figures,	1
Sines,	7
Small Angles, Sines and Tangents of,	
Squares,	6
Square Roots,	
Speeds of Pulleys,	1
Steam Engine,	
Surveying,	2
Tangents,	7
Teeth, Gear Wheels,	
Test Problems,	9
Thermometer,	8
Triangles, Solution by Slide Rule,	8
Turbine,	1
Water Velocity,	1
Wind, Force of,	9

# SLIDE RULES FOR MANY PURPOSES.

In addition to our extended line of regular Mannheim and Duplex Slide Rules, we manufacture a variety of rules for special purposes, of which we name a few below:

### THE ROYLANCE ELECTRICAL SLIDE RULE



This rule is a modification of our regular Slide Rule No. 4035 and can be used for all the calculations made with the ordinary Slide Rule. In addition to the usual scales, it carries a series of scales or gauge marks by means of which the different properties of copper wire, such as size, conductivity, weight, etc., may be determined without the use of tables. It also carries the  $CI_1$  or inserted  $CI_2$  scale.

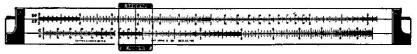
## SURVEYOR'S DUPLEX SLIDE RULE



The fact that all astronomical data essential to surveying, such as azimuth, time, latitude, etc., can be ascertained by means of the usual type of Transit with vertical circle but without solar attachment, while generally known, is rather seldom utilized in this country. The main reason for this surprising condition is the difficulty of computing, in the field, by spherical tr gonometry, the results of observations.

The new K & E Surveyors' Slide Rule entirely eliminates this difficulty by reducing the hitherto complicated calculations to mere mechanical operations, thereby rendering the method of field astronomy with the regular Engineer's Transit extremely simple and practical.

## MERCHANT'S (CALCULATING) SLIDE RULE



Especially designed for the merchant, importer, exporter, accountant, manager, mechanic, foreman, etc. By means of it, all manner of problems involving multiplication, division and proportion can be correctly solved without mental strain and in a small fraction of the time required to work them out by the usual "figuring".

### THE CHEMIST'S DUPLEX SLIDE RULE

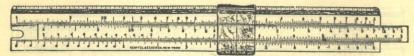


For the rapid solution of problems in Stoichiometry, such as Gravimetric and Volumetric Analysis, Equivalents, Percentage Composition, Conversion Factors and many others,

# SLIDE RULES OF ALL KINDS.

We are the largest manufacturers of slide rules in America and have the largest assortment. Some of the best known of our slide rules are shown below.

#### MANNHEIM



Mannheim Slide Rules can be used to advantage in every line of business. They have our patent adjustment for obtaining any desired friction of the slide.

#### POLYPHASE

	100		
	0	1 0	A STATE OF THE PARTY OF THE PAR
	T.	la Falala	Laboration of the state of the
CI washing and a supplemental an	The second	T. Sanda	and the state of t
	1	بالتليليان	hard to the transfer of the state of the sta
K salatabahahahahahahahahahahahahahahahahahah	5 7	23.2	THE RESIDENCE AND ASSESSED.
	O	1 0	

The Polyphase Slide Rule is of the Mannheim type, but has an inverted C scale and a scale of cubes in addition to the regular M annheim scales. This arrangement facilitates the solution of many problems involving three factors, as well as many powers and roots,

#### POLYPHASE DUPLEX

danis	terfficurisming dame underwitte of faitnesses also farities and destrict one of	Balance
	DF 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	M
4088	C15 C2	
6	C to the state of	
	D	
- 5200	Out on the	SHEAR)

The Polyphase Duplex Slide Rules are a combination of the Polyphase and the Duplex Rules, with the addition of several special scales.

### LOG LOG DUPLEX

		9	0		
9.	LLO MILLION MARKET LILLION DE LA CONTRACTION DEL CONTRACTION DE LA CONTRACTION DE LA CONTRACTION DE LA CONTRACTION DE LA CONTRACTION DEL CONTRACTION DE LA C	19 197.	.7.,		
	2	ALIMATE .			
4	C local bandle with a free free free free free free free fr	Septiment of the septim	ingophylo of supplyings	Tomorphological Company	
0	Trifficial mandemarked and an interest of the state of th	edantabilit	and grithin	antenial topinal Transpilling	

The Log Log Duplex Slide Rule has in addition to the scales of the regular Polyphase Duplex slide rule, Log Log scales, with which roots and powers may be determined by direct operation at one setting of the slide.

# K & E STADIA SLIDE RULE

10 20 20 20 40 40 40 40 40 100 100 100 100 200 100 200 100 100 10	300	1400 506 600 and 1000
The state of the s	250 20	35 05 2 0 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Lundrentraden den den der eine eine den den den den den den den den den d	india 4.2	40 50 60 so too

This form of Stadia Slide Rule is remarkable for its simplicity. By one setting of the slide the horizontal distance and vertical height can be obtained at once when the stadia rod reading and the angle of elevation or depression of the telescope are known.